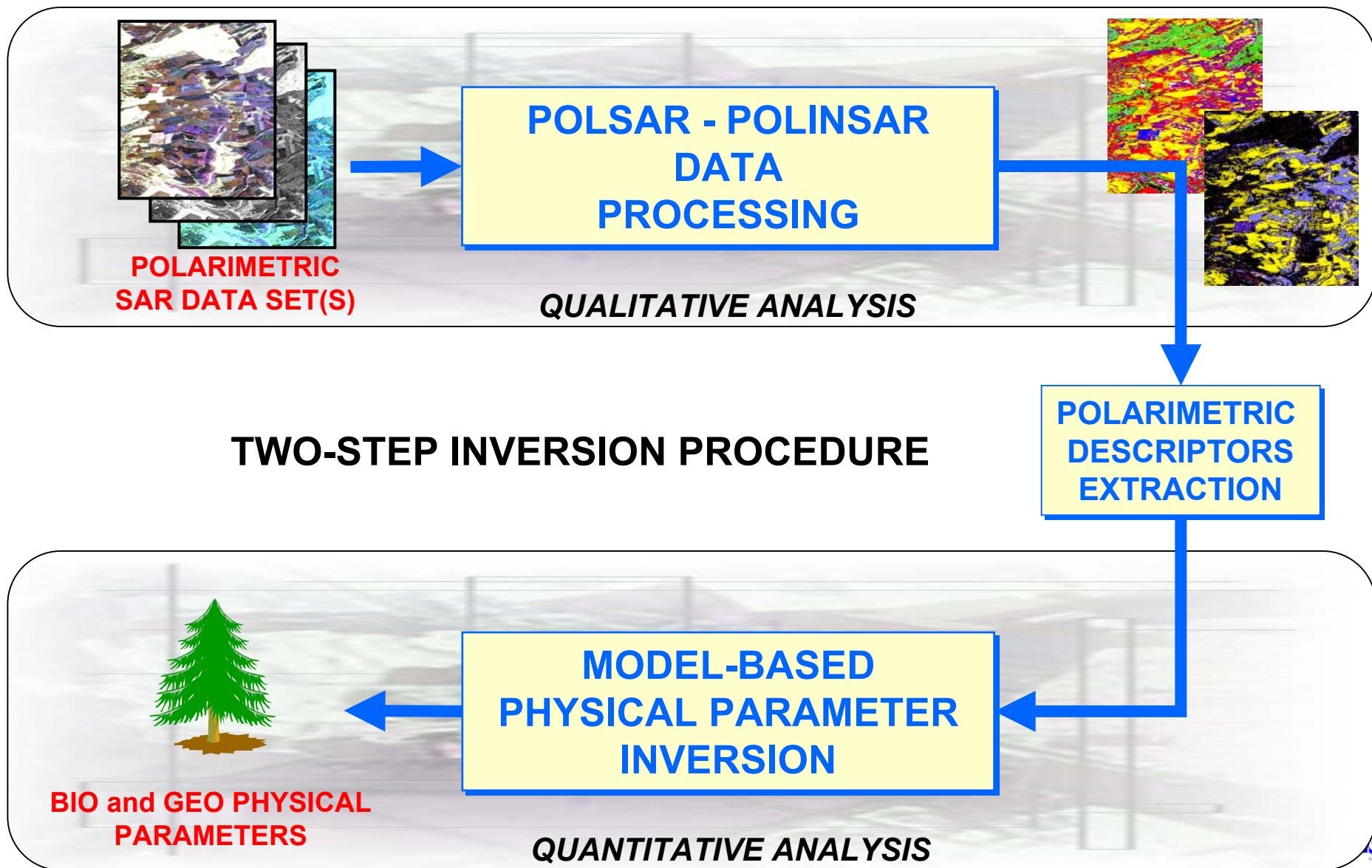
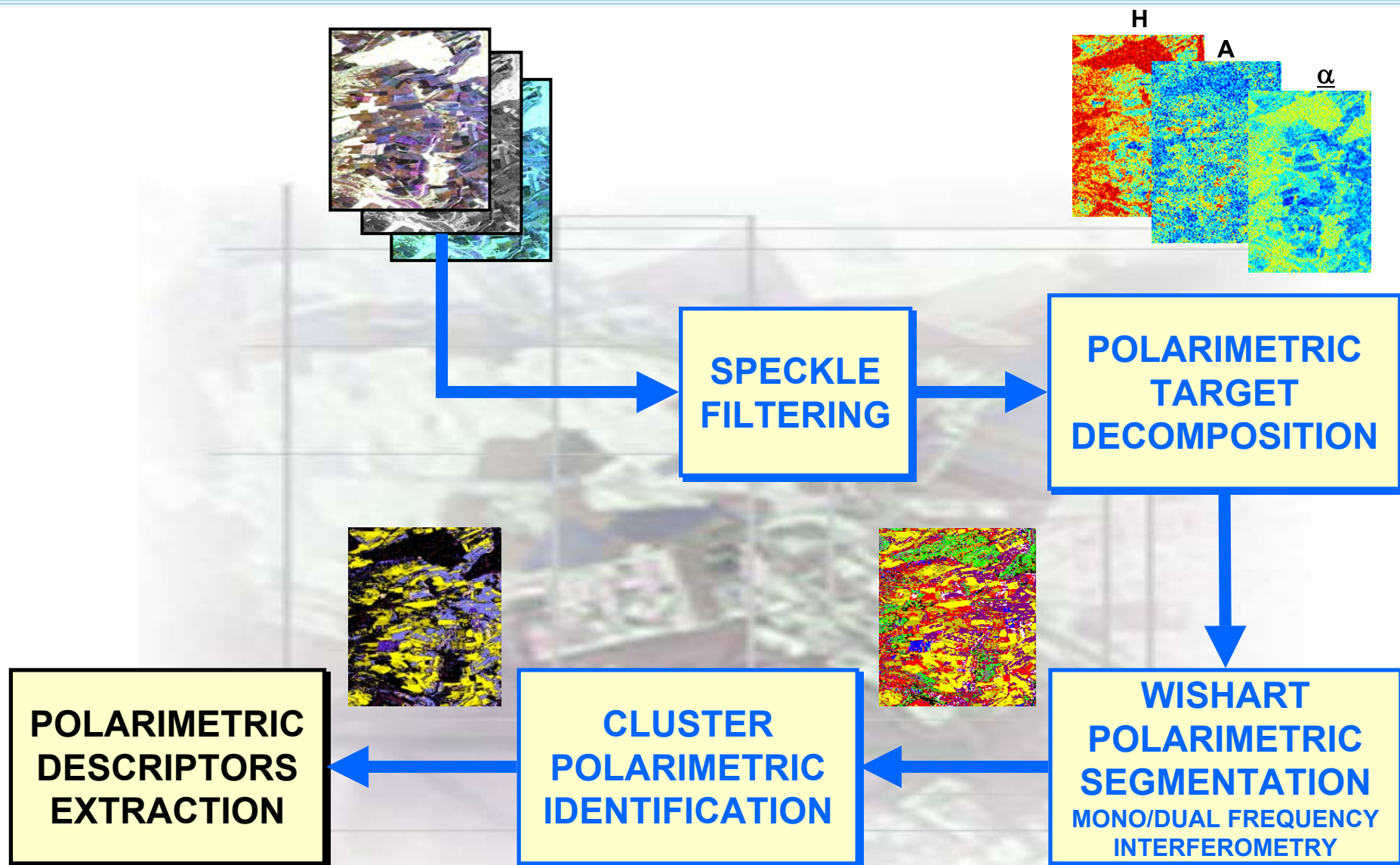
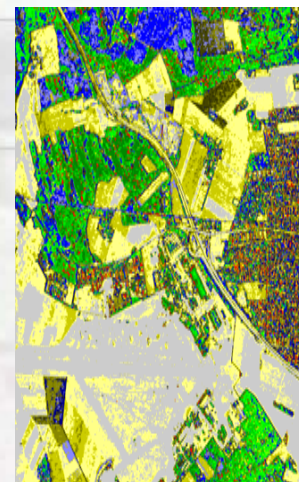
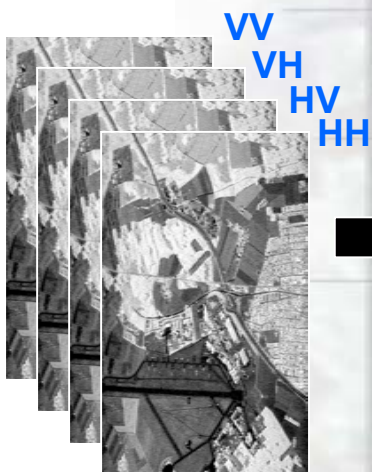


# POL-SAR CLASSIFICATION





WISHART PDF  $P(\langle [T] \rangle / [T_m]) = \frac{L^L p \langle [T] \rangle^{L-p} e^{-L \text{Tr}([T_m]^{-1} \langle [T] \rangle)}}{\pi^{\frac{p(p-1)}{2}} \Gamma(L) \dots \Gamma(L-p+1) [T_m]^L}$



## Target Vector

$$\underline{X} = \begin{bmatrix} \mathbf{S}_{HH} & \sqrt{2}\mathbf{S}_{HV} & \mathbf{S}_{VV} \end{bmatrix}^T$$

$$P(\underline{X}) = \frac{1}{\pi^3 \|\mathbf{C}\|} e^{-\underline{X}^{*T} [\mathbf{C}]^{-1} \underline{X}}$$

$$\underline{k} = \frac{1}{\sqrt{2}} \begin{bmatrix} \mathbf{S}_{HH} + \mathbf{S}_{VV} & \mathbf{S}_{HH} - \mathbf{S}_{VV} & 2\mathbf{S}_{HV} \end{bmatrix}^T$$

$$P(\underline{k}) = \frac{1}{\pi^3 \|\mathbf{T}\|} e^{-\underline{k}^{*T} [\mathbf{T}]^{-1} \underline{k}}$$

## Coherency Matrix

$$\langle [\mathbf{T}] \rangle = \frac{1}{N} \sum_{i=1}^N \underline{k}_i \cdot \underline{k}_i^{*T} = \frac{1}{N} \sum_{i=1}^N [\mathbf{T}_i]$$

$$P(\langle [\mathbf{T}] \rangle / [\mathbf{T}_m]) = \frac{L^{Lp} \|\langle [\mathbf{T}] \rangle\|^{L-p} e^{-L \text{Tr}([\mathbf{T}_m]^{-1} \langle [\mathbf{T}] \rangle)}}{\pi^{\frac{p(p-1)}{2}} \Gamma(L) \dots \Gamma(L-p+1) \|\mathbf{T}_m\|^L}$$

## COMPLEX WISHART DISTRIBUTION

L: Number of Look      p: Polarimetric Dimension

$$P(\langle [T] \rangle / [T_m]) = \frac{L^{Lp} \|\langle [T] \rangle\|^{L-p} e^{-LTr([T_m]^{-1} \langle [T] \rangle)}}{\pi^{\frac{p(p-1)}{2}} \Gamma(L) \dots \Gamma(L-p+1) [T_m]^L}$$



## SUPERVISED WISHART CLASSIFIER (Lee 1994)

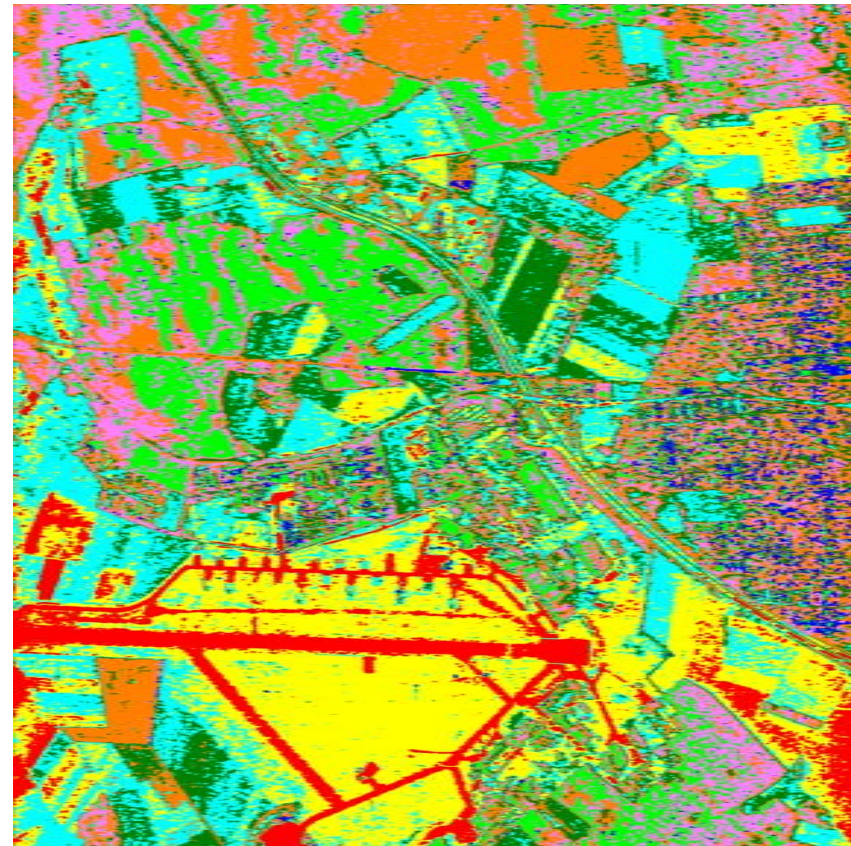
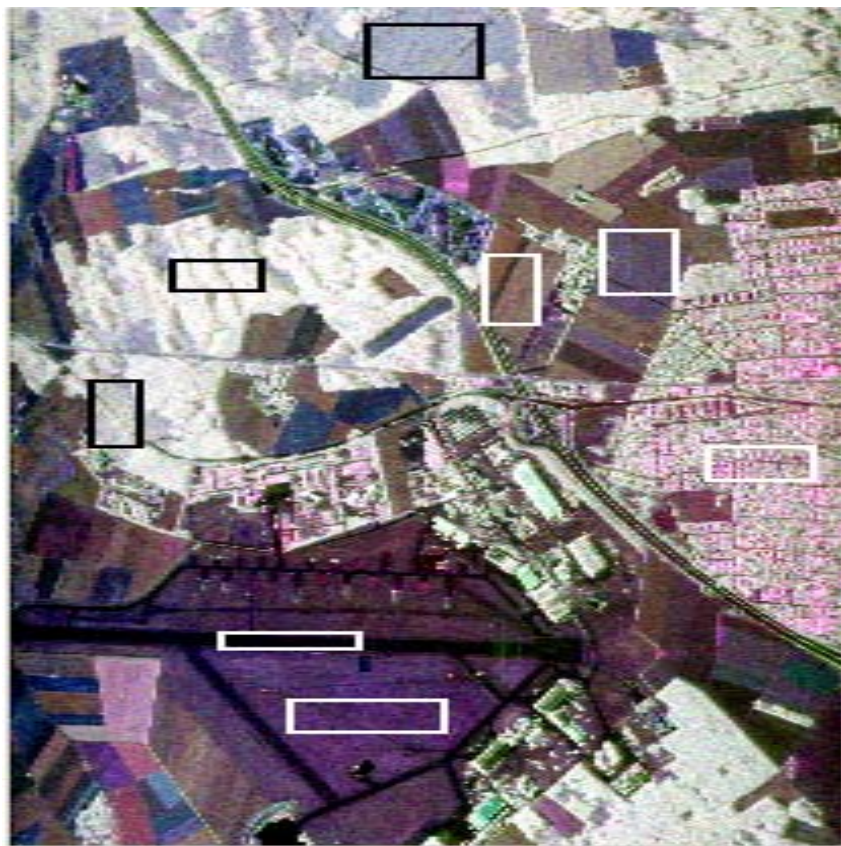
### BAYES MAXIMUM LIKELIHOOD CLASSIFICATION PROCEDURE

$$\langle [T] \rangle \in [T_m] \quad \text{if} \quad d_m(\langle [T] \rangle) < d_j(\langle [T] \rangle) \quad \forall j \neq m$$

with

$$d_m(\langle [T] \rangle) = LTr([T_m]^{-1} \langle [T] \rangle) + L \ln(\| [T_m] \|) - \ln(P([T_m])) + K$$

$[T_m]$  : Cluster Center of the class  $m$

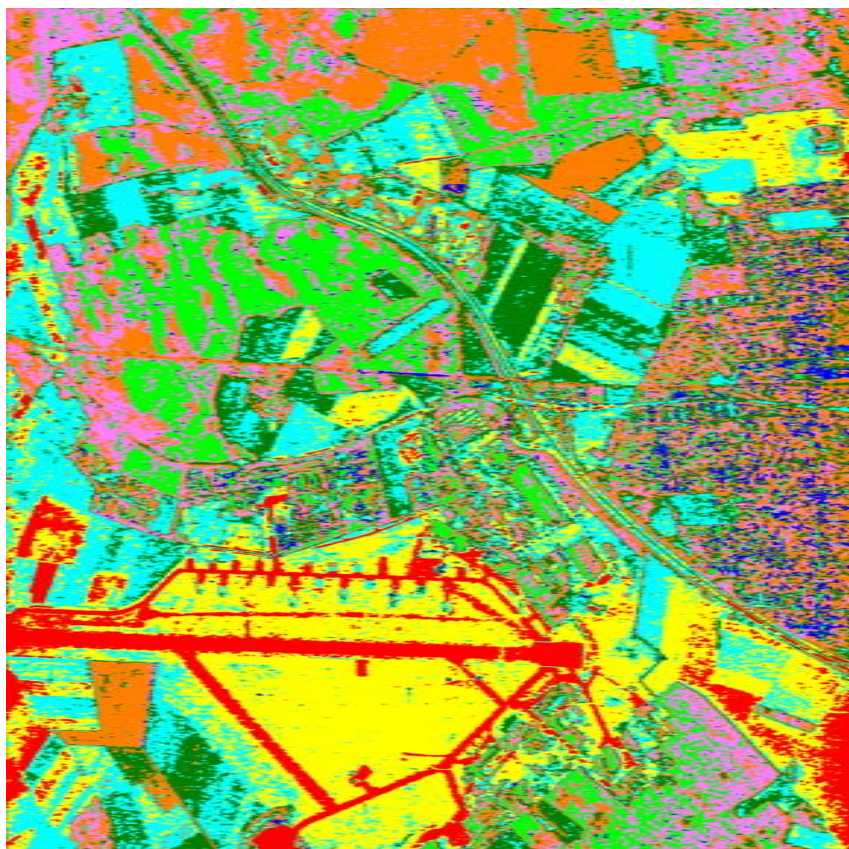


$2A_0$

$B_0 + B$

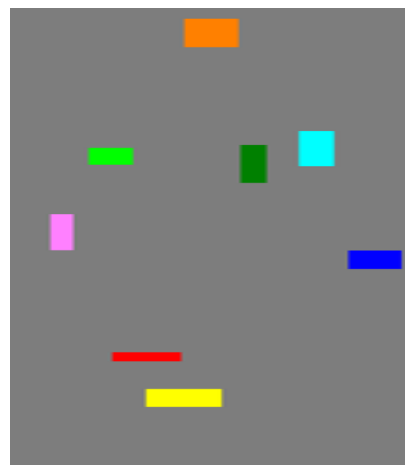
$B_0 - B$

## FULLY POLARIMETRIC DATA CLASSIFICATION



Fully polarimetric coherent data segmentation

### Training areas definition quality



User defined training areas



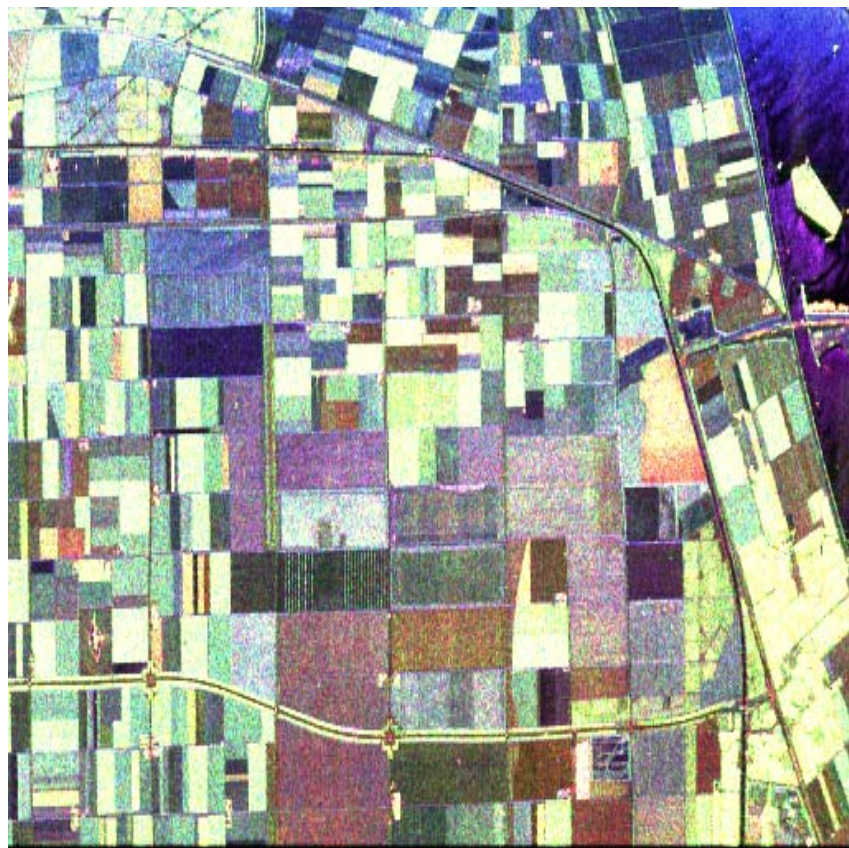
Classified training areas



### CONFUSION MATRIX



Courtesy of Dr J.S Lee



$2A_0$

$B_0 + B$

$B_0 - B$

JPL AIRSAR  
P-L-C Band Flevoland Data



- |             |            |            |
|-------------|------------|------------|
| ■ Stenbeans | ■ Lucerne  | ■ Rapeseed |
| ■ Forest    | ■ Wheat    | ■ Peas     |
| ■ Water     | ■ Baresoil | ■ Grass    |
| ■ Potatoes  | ■ Beet     |            |

Original Ground- Truth



Training Sets / Reference map

Courtesy of Dr J.S Lee



$2A_0$

$B_0 + B$

$B_0 - B$

JPL AIRSAR  
L-Band Flevoland Data



C-band (66.53%)

Courtesy of Dr J.S Lee



$2A_0$

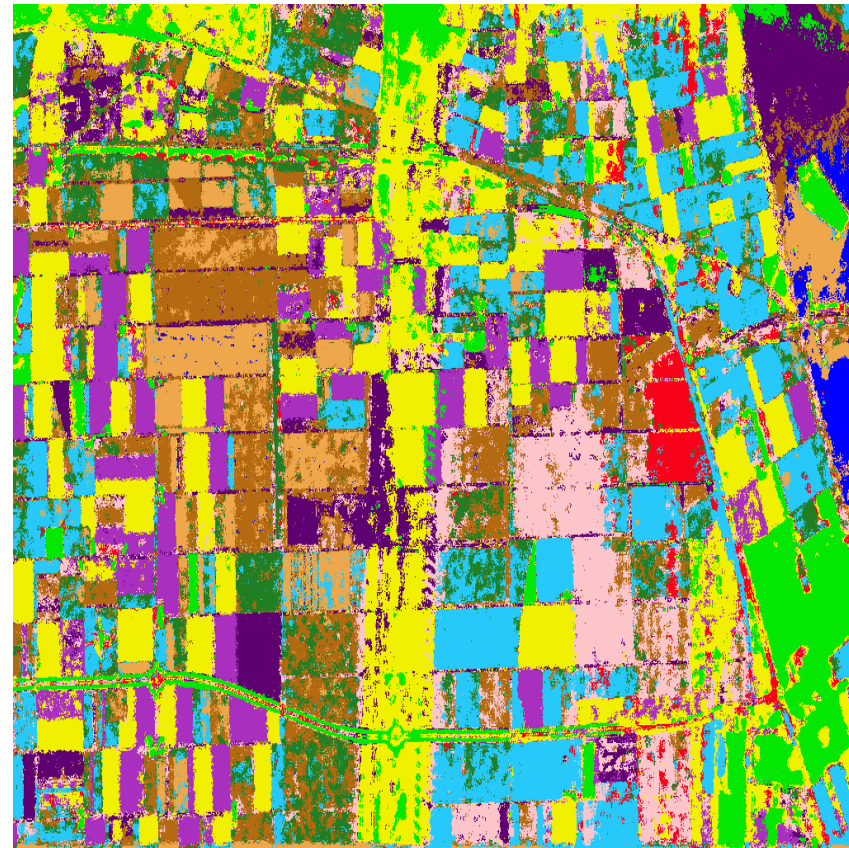
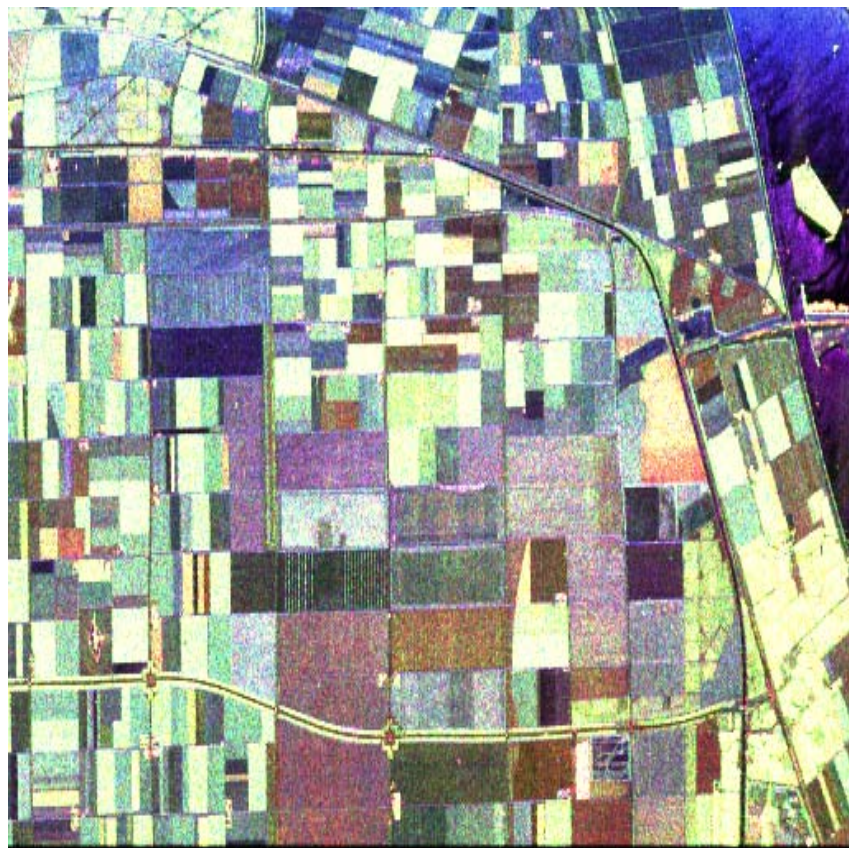
$B_0 + B$

$B_0 - B$

L-band (81.63%)

JPL AIRSAR  
L-Band Flevoland Data

Courtesy of Dr J.S Lee



$2A_0$

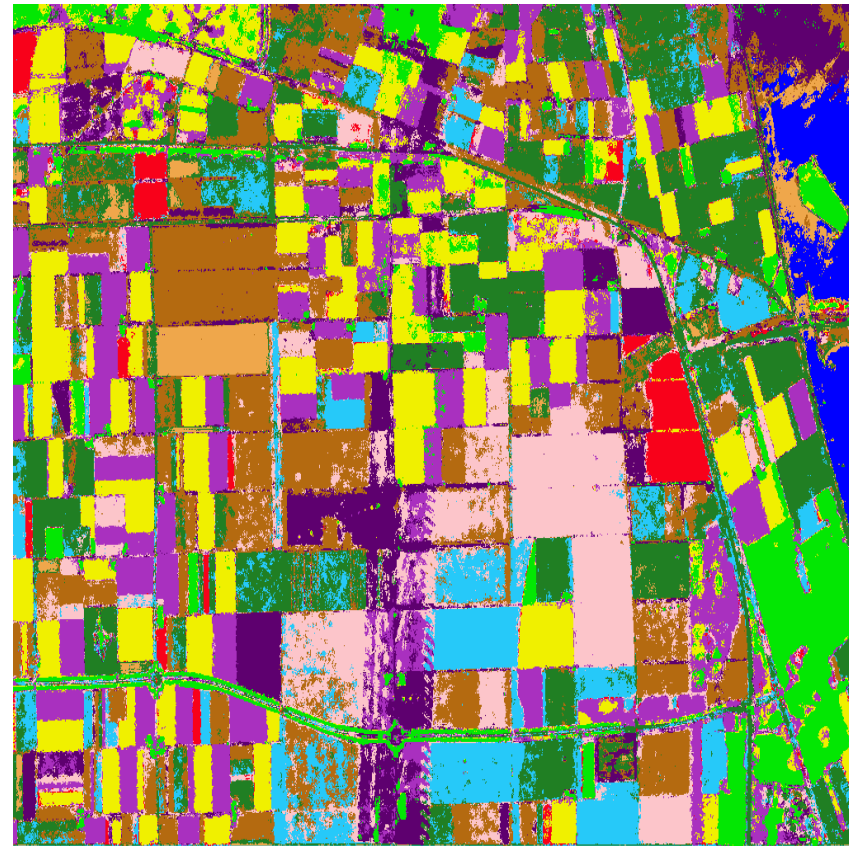
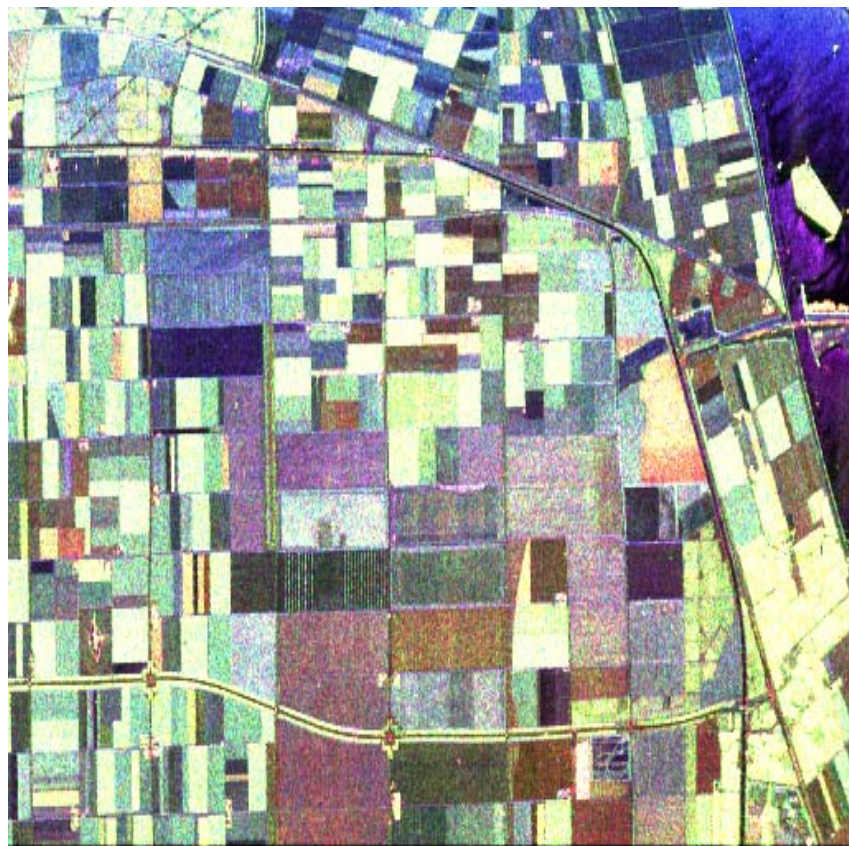
$B_0 + B$

$B_0 - B$

P-band (71.37%)

JPL AIRSAR  
L-Band Flevoland Data

Courtesy of Dr J.S Lee



$2A_0$

$B_0 + B$

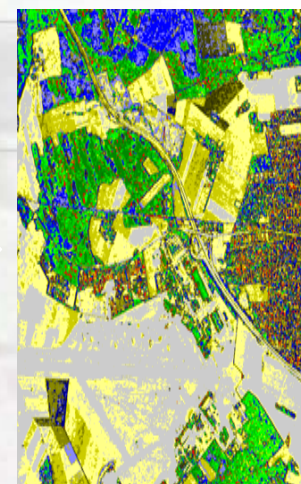
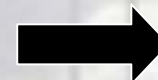
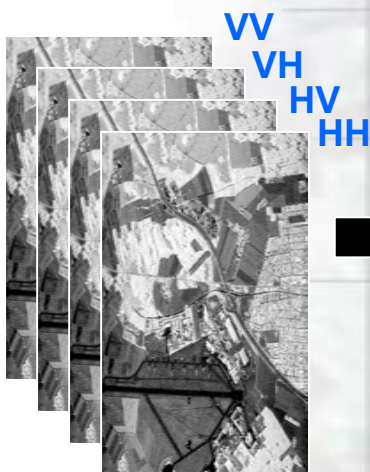
$B_0 - B$

P-L-C band (91.21%)

JPL AIRSAR  
L-Band Flevoland Data

WISHART PDF

$$P(\langle [T] \rangle / [T_m]) = \frac{L^p \|\langle [T] \rangle\|^{L-p} e^{-L \text{Tr}([T_m]^{-1} \langle [T] \rangle)}}{\pi^{\frac{p(p-1)}{2}} \Gamma(L) \dots \Gamma(L-p+1) [T_m]^L}$$



## Quantitative Comparison Fully Polarimetric versus Dual Polarizations

J.S. Lee, M. R. Grunes and E. Pottier, "Quantitative Comparison of Classification Capability: Fully polarimetric versus Dual- and Single polarization SAR," IEEE TGRS, November 2002

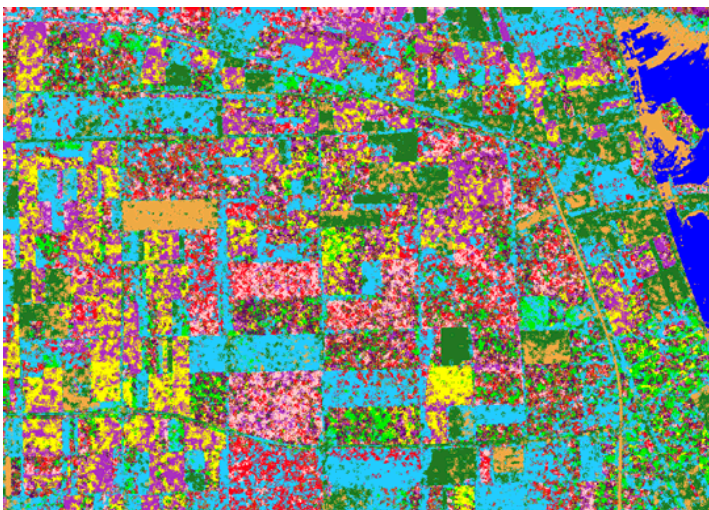
Courtesy of Dr J.S Lee



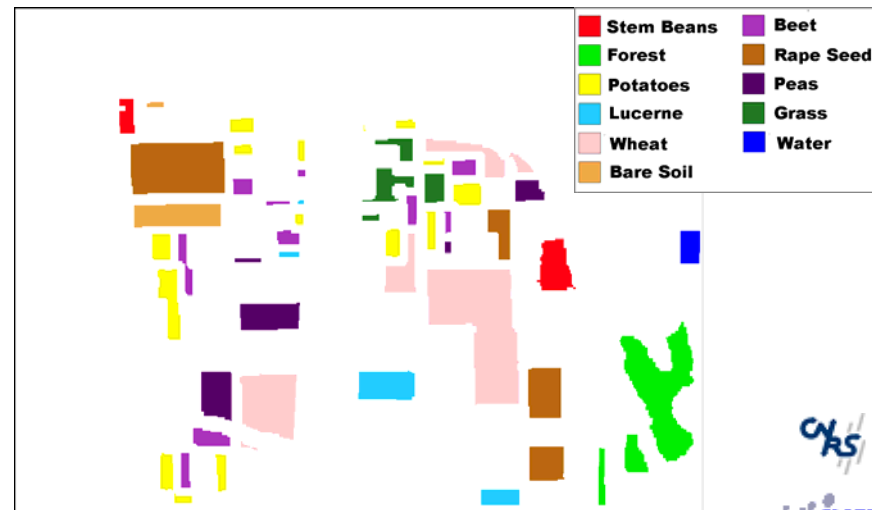
C-band Fully Pol. (66.55%)



C-band complex HH and VV (55.00%)



C-band HH and VV Intensities (37.22%)



Reference map for comparison

Courtesy of Dr J.S Lee



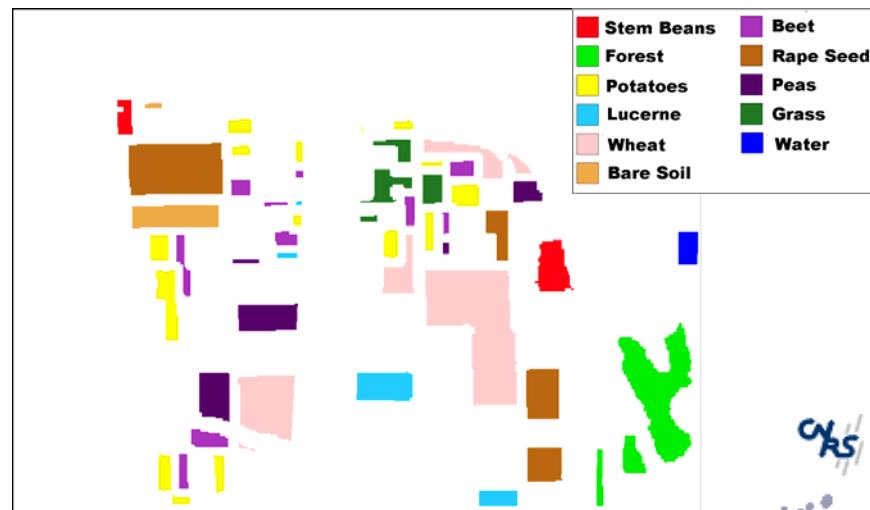
L-band Fully Pol. (81.63%)



L-band complex HH and VV (80.91%)



L-band HH and VV Intensities (56.35%)



Reference map for comparison

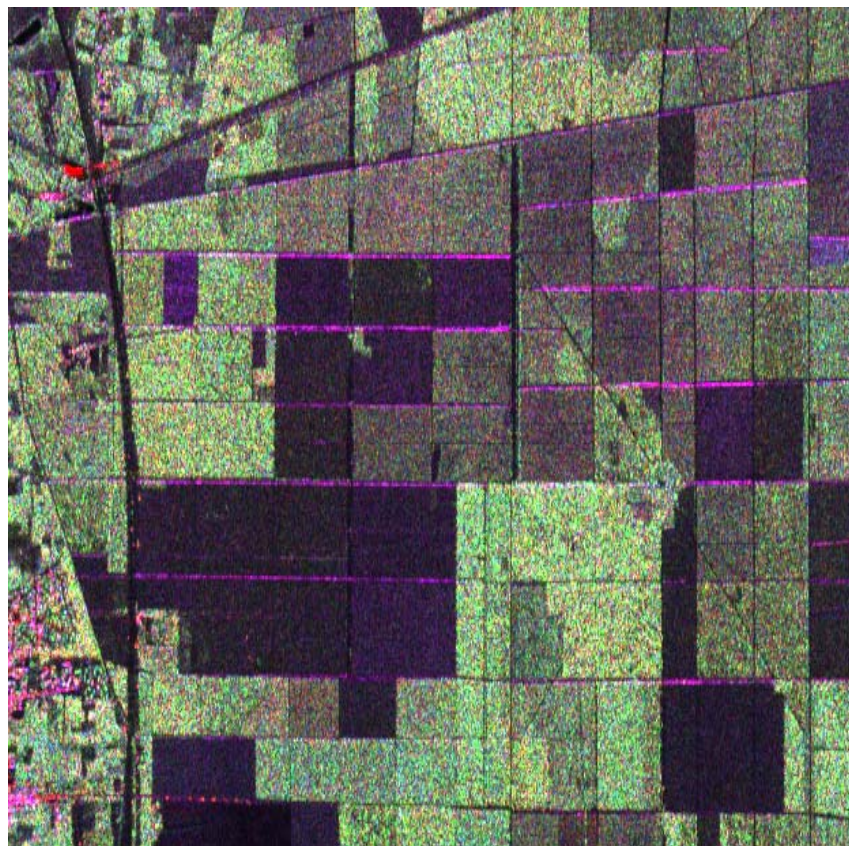


Courtesy of Dr J.S Lee

	Fully Polarimetric	Complex HH, HV	Intensity HH, HV	Complex HH, VV	Intensity HH, VV	Complex VV, HV	Intensity VV, HV
Stem Bean	<b>95.32</b>	<b>51.16</b>	<b>63.27</b>	<b>90.64</b>	<b>61.73</b>	<b>35.97</b>	<b>31.29</b>
Forest	<b>81.07</b>	<b>66.73</b>	<b>68.39</b>	<b>75.75</b>	<b>33.83</b>	<b>60.05</b>	<b>60.91</b>
Potatoes	<b>82.89</b>	<b>67.53</b>	<b>66.36</b>	<b>81.52</b>	<b>49.35</b>	<b>54.40</b>	<b>59.15</b>
Lucerne	<b>97.91</b>	<b>39.29</b>	<b>38.23</b>	<b>99.26</b>	<b>65.15</b>	<b>67.49</b>	<b>65.30</b>
Wheat	<b>64.80</b>	<b>49.77</b>	<b>44.27</b>	<b>68.02</b>	<b>53.72</b>	<b>49.43</b>	<b>41.65</b>
Bare Soil	<b>99.36</b>	<b>90.04</b>	<b>82.86</b>	<b>98.42</b>	<b>93.15</b>	<b>90.93</b>	<b>63.74</b>
Beet	<b>89.26</b>	<b>68.80</b>	<b>66.36</b>	<b>86.22</b>	<b>81.98</b>	<b>75.94</b>	<b>74.77</b>
Rape Seed	<b>89.05</b>	<b>55.01</b>	<b>53.23</b>	<b>87.18</b>	<b>49.85</b>	<b>82.31</b>	<b>77.12</b>
Peas	<b>86.47</b>	<b>50.77</b>	<b>39.25</b>	<b>84.59</b>	<b>65.21</b>	<b>81.82</b>	<b>79.59</b>
Grass	<b>91.05</b>	<b>66.44</b>	<b>65.06</b>	<b>90.13</b>	<b>71.08</b>	<b>75.36</b>	<b>75.19</b>
Water	<b>100</b>	<b>90.39</b>	<b>87.33</b>	<b>100</b>	<b>99.86</b>	<b>96.30</b>	<b>70.53</b>
<b>TOTAL</b>	<b>81.63</b>	<b>59.16</b>	<b>55.38</b>	<b>80.91</b>	<b>56.35</b>	<b>64.72</b>	<b>60.12</b>

## L-Band Crop Classification Results

Courtesy of Dr J.S Lee



$2A_0$

$B_0 + B$

$B_0 - B$

JPL AIRSAR

P-L-C Band Nezer Forest Data



Yellow Bare soil

Red 15-19 years

Blue 5-8 years

Green 33-41 years

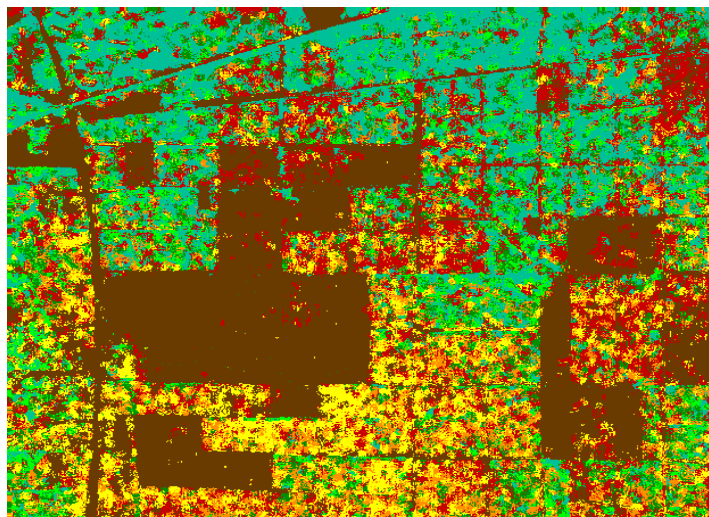
Cyan 8-11 years

Dark Green > 41 years

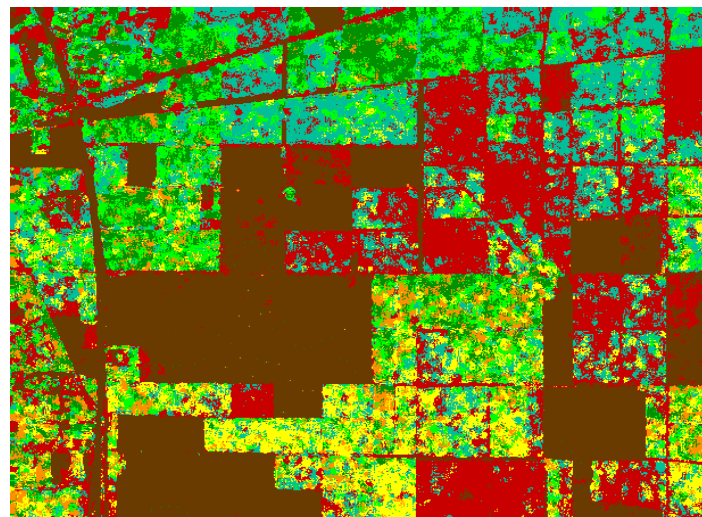
Pink 11-14 years

White N / A

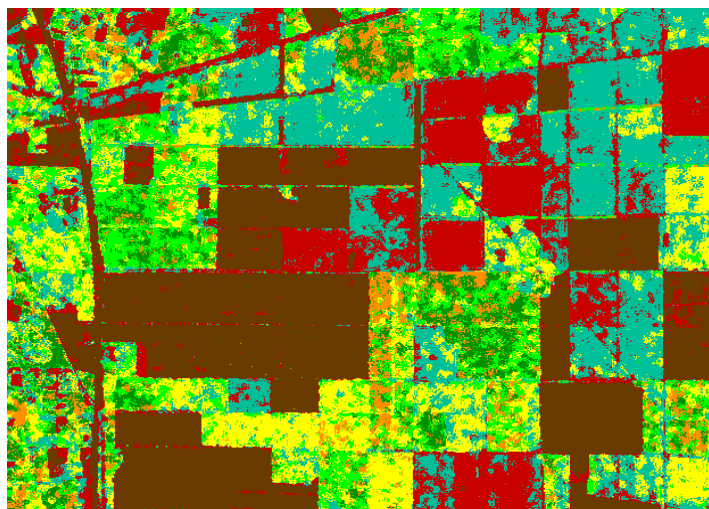
Courtesy of Dr J.S Lee



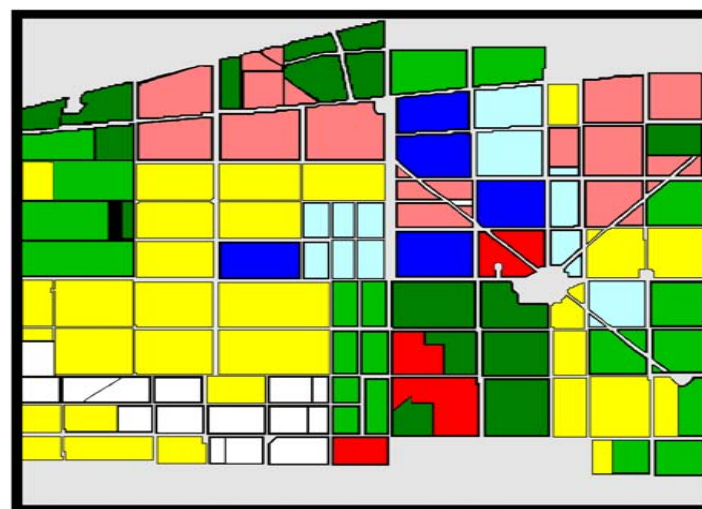
C-band Fully Polarimetric (42.96%)



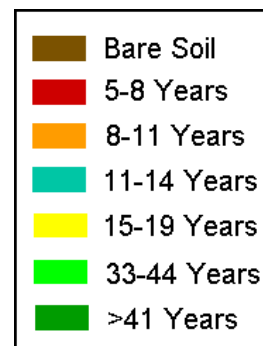
L-band Fully Polarimetric (64.68%)



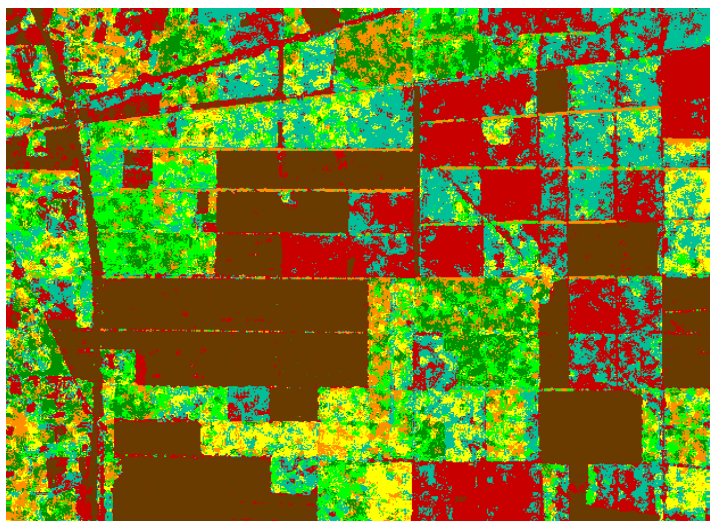
P-band Fully Polarimetric (79.16%)



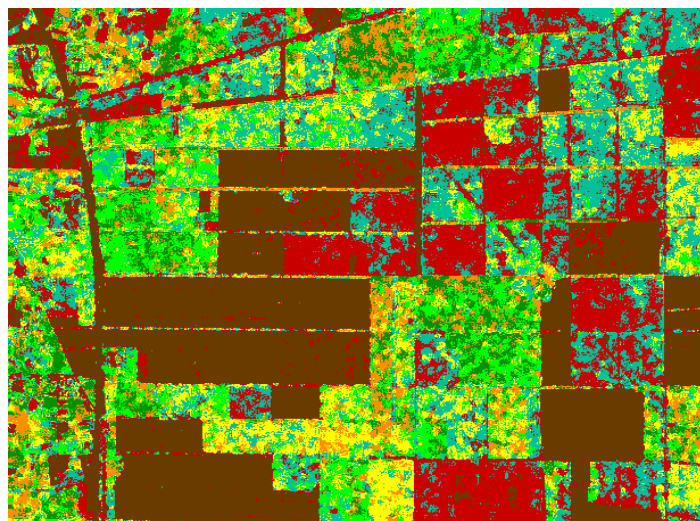
Reference Map



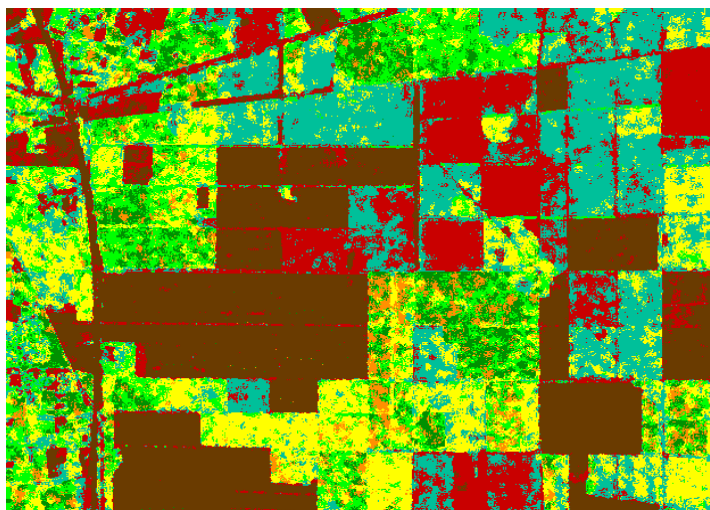
Courtesy of Dr J.S Lee



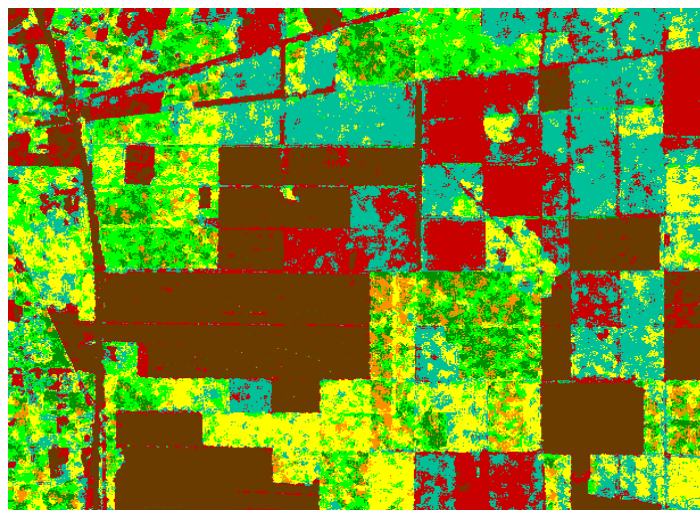
**P-band Complex HH and VV (68.56%)**



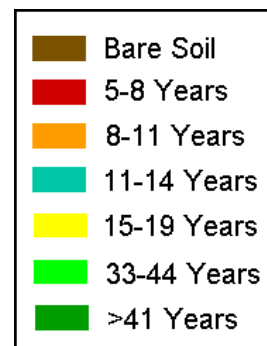
**P-band Intensity HH and VV (65.30%)**



**P-band Complex HH and HV (75.95%)**

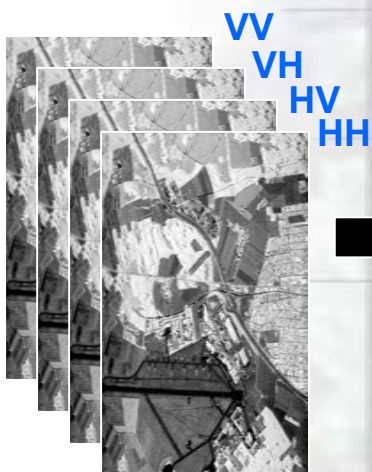


**P-band Intensity HH and HV (75.44%)**

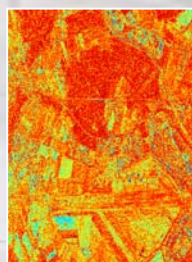
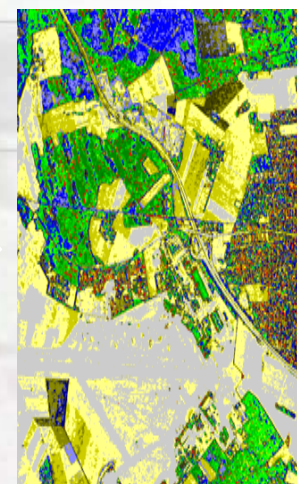


- **For crop classification**
  - L-band is better than P-Band and C-band
  - Dual-pol HH and VV with coherence (Including phase differences) is almost as good as fully polarimetric
- **For forest classification**
  - P-band is better than L and C
  - HV is the most important polarization
  - Coherence is not important for classification

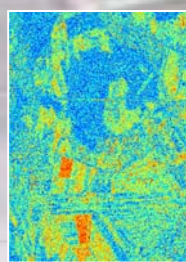
**WISHART PDF**  $P(\langle [T] \rangle / [T_m]) = \frac{L^p \langle [T] \rangle^{L-p} e^{-L \text{Tr}([T_m]^{-1} \langle [T] \rangle)}}{\pi^{\frac{p(p-1)}{2}} \Gamma(L) \dots \Gamma(L-p+1) [T_m]^L}$



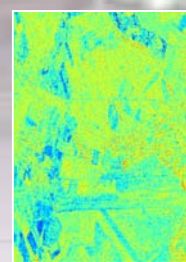
**UNSUPERVISED  
POLARSAR  
CLASSIFICATION**  
E.POTTIER, J.S LEE (2000)



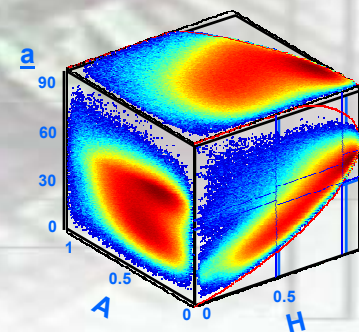
H



A

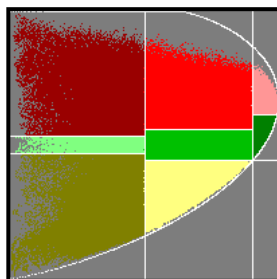
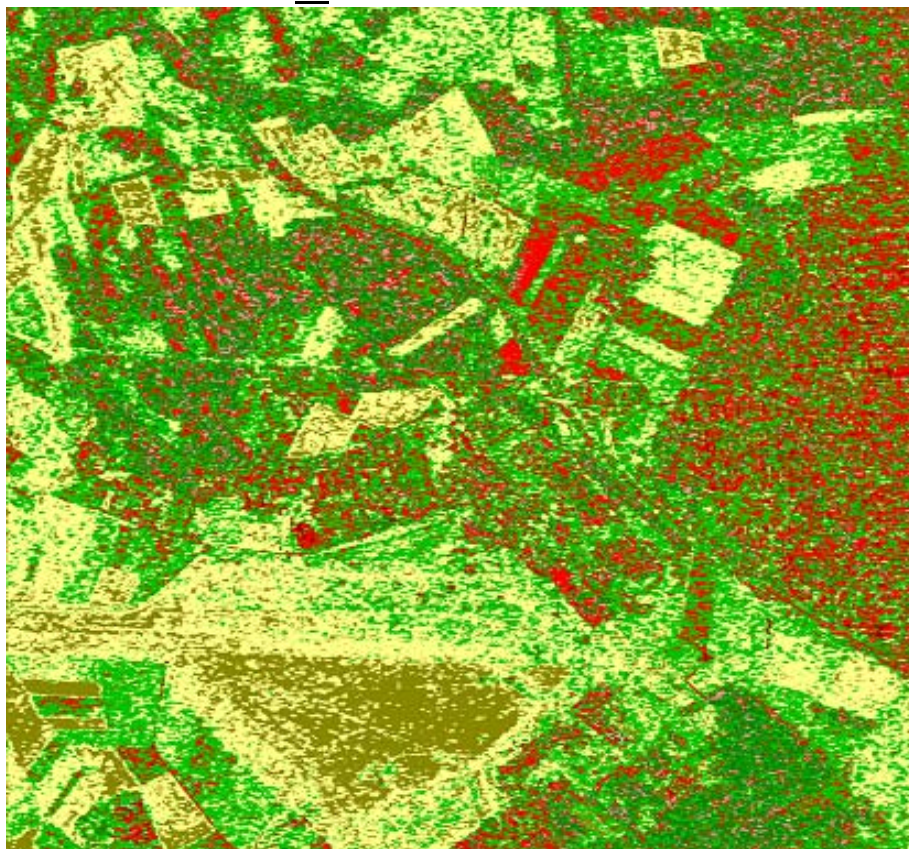


$\alpha$



**H / A /  $\alpha$  DECOMPOSITION THEOREM**

## H- $\alpha$ classification



H /  $\alpha$  Classification Space  
Sub-divided into 9 basic zones



Location of the boundaries  
is arbitrary and generically

Degree of arbitrariness on the  
setting of these boundaries



Segmentation is offered merely  
to illustrate the unsupervised  
classification strategy and to  
emphasize the geometrical  
segmentation of physical scattering  
processes

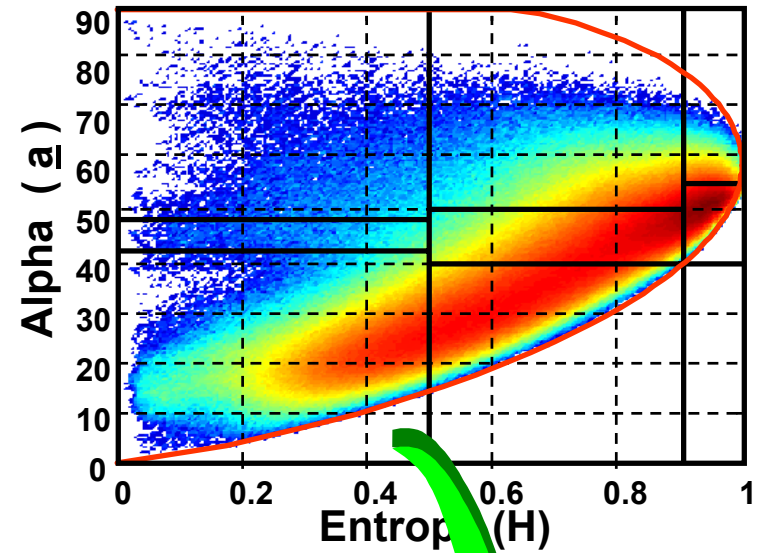
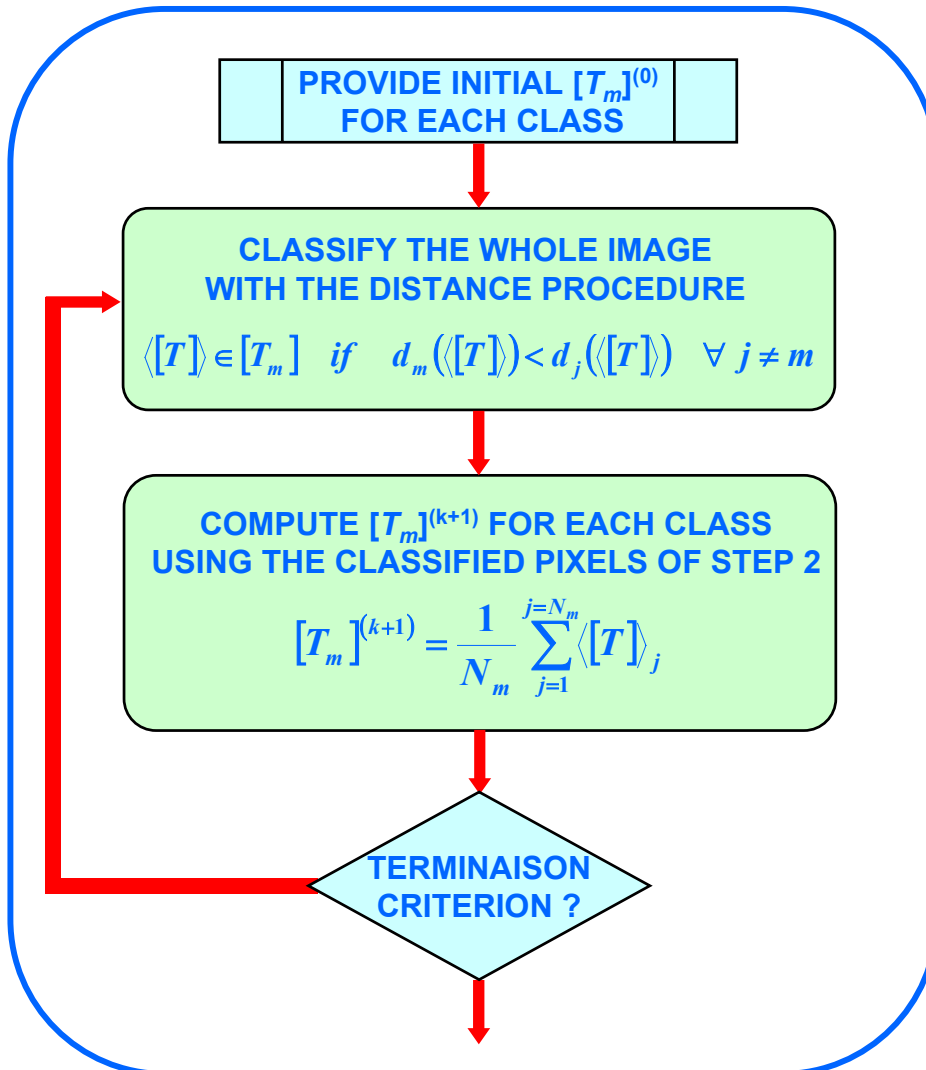


Dr J.S. LEE  
N.R. L US -NAVY

- 1994** *LEE et al.* PROPOSED A SUPERVISED ALGORITHM BASED ON THE COMPLEX WISHART DISTRIBUTION FOR THE COMPLEX COVARIANCE / COHERENCY MATRIX.
- 1998** *LEE et al.* DEVELOPED A COMBINED UNSUPERVISED CLASSIFICATION METHOD THAT USES THE H /  $\alpha$  PLANE WHICH INITIALLY CLASSIFIES THE POLSAR IMAGE. THIS SEGMENTED IMAGE IS THEN USED AS TRAINING SETS FOR THE INITIALIZATION OF THE SUPERVISED WISHART CLASSIFIER.
- 1999** INTRODUCTION OF THE ANISOTROPY (*E. POTTIER - J.S.LEE*) IMPROVEMENT OF THE CAPABILITY TO DISTINGUISH BETWEEN DIFFERENT CLASSES WHOS CENTERS END IN THE SAME ENTROPY (H) AND ALPHA ( $\alpha$ ) ZONE.



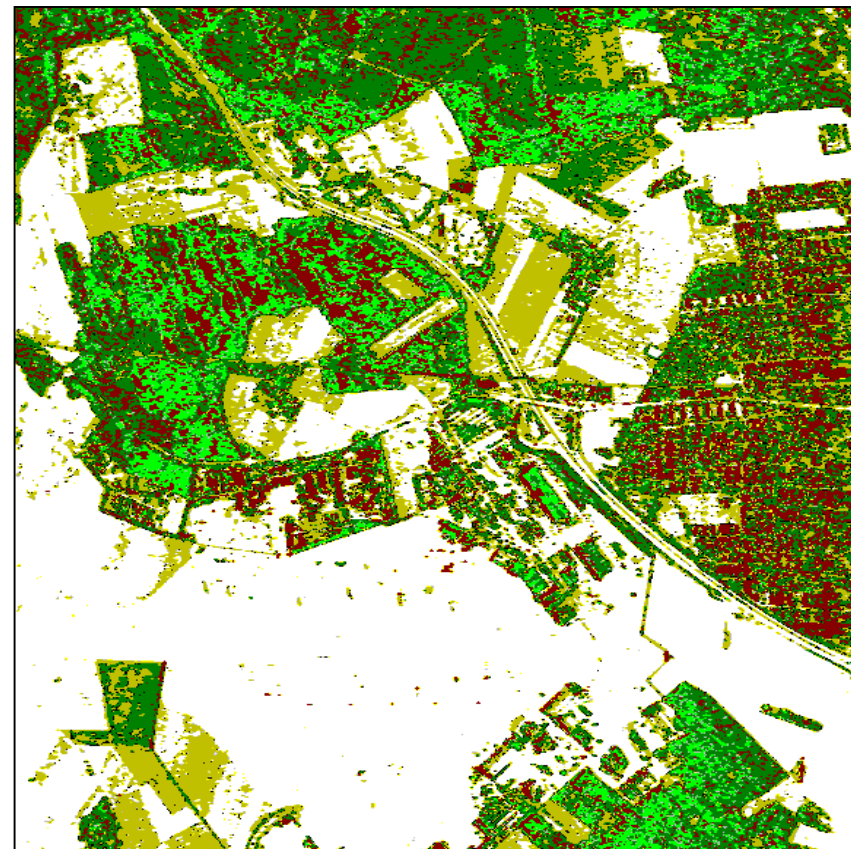
## k - mean CLASSIFICATION PROCEDURE



$$[T_m]^{(0)} = \frac{1}{N_m} \sum_{k=1}^{k=N_m} \langle [T] \rangle_k$$

Cluster Center of the class  $m$   
(Lee 1998)

4th ITERATION



$2A_0$

$B_0 + B$

$B_0 - B$

C1

C2

C3

C4

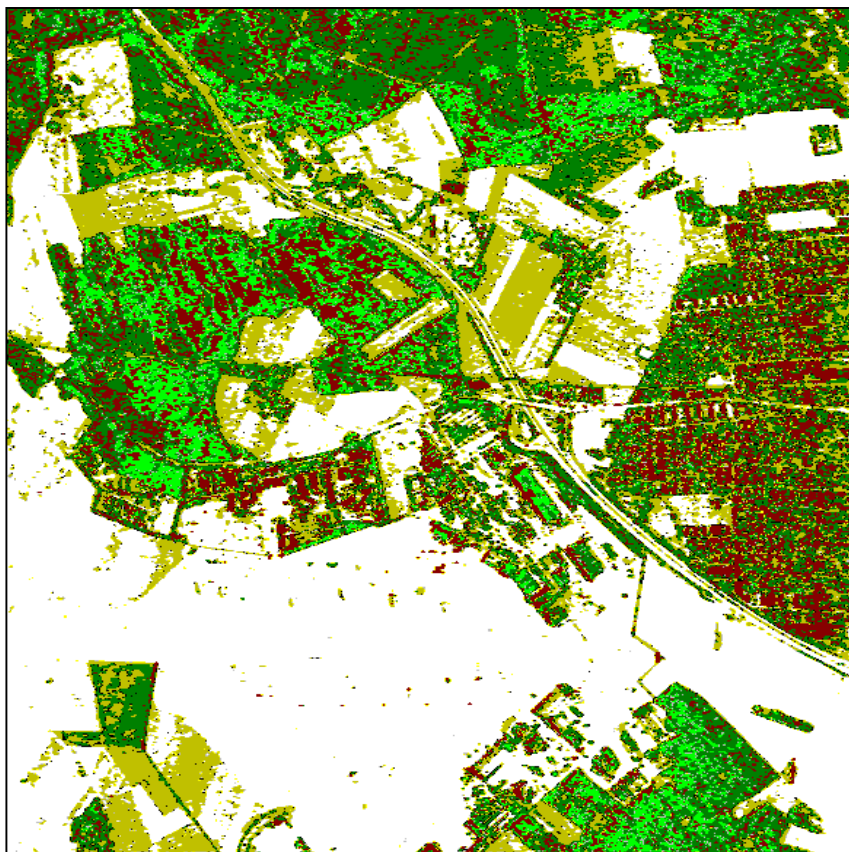
C5

C6

C7

C8





C1 C2 C3 C4 C5 C6 C7 C8



During the classification, the cluster centers can move out their zones or several clusters may end in the same zone



Identification of the terrain type may cause some confusion due to the color scheme

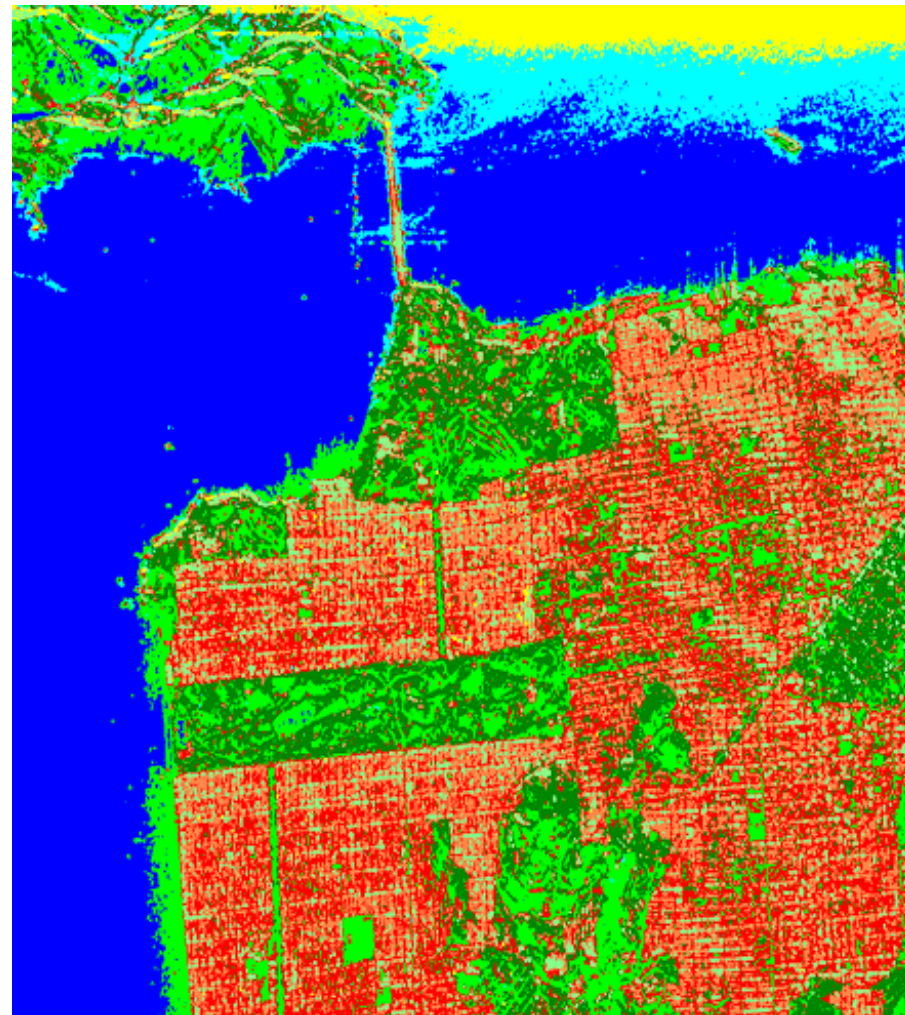


The combined Wishart classifier is extended and complemented with the introduction of the Anisotropy (A)

SAN FRANCISCO BAY JPL - AIRSAR L-band 1988



H /  $\alpha$  and WISHART CLASSIFIER



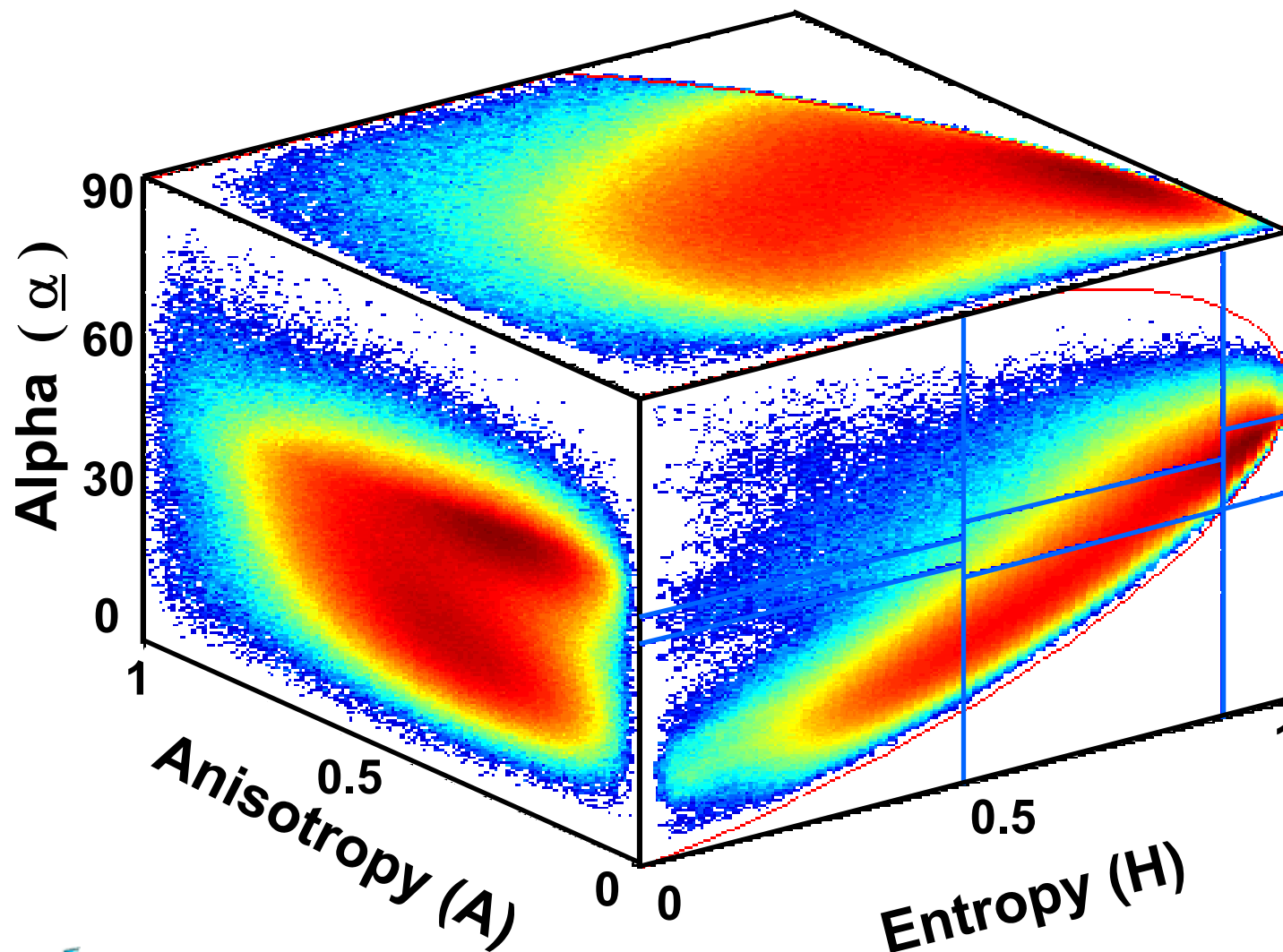
$2A_0$

$B_0 + B$

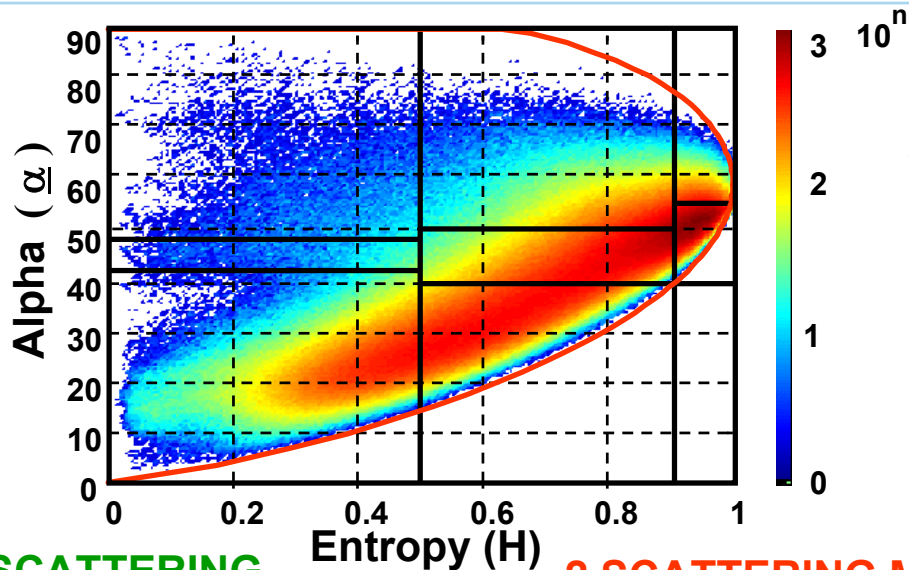
$B_0 - B$



## POLSAR DATA DISTRIBUTION IN THE H / A / $\alpha$ SPACE



**A < 0.5**  
 $\lambda_2 \approx \lambda_3$

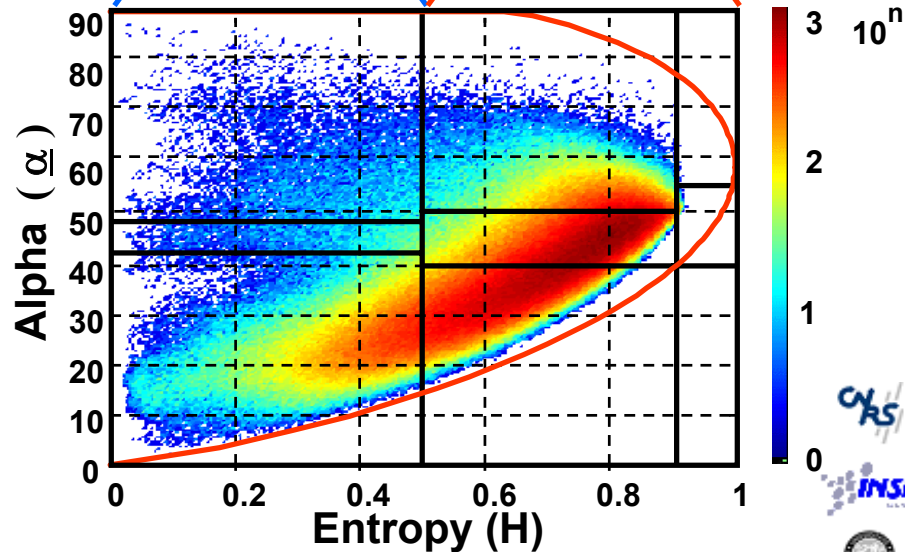
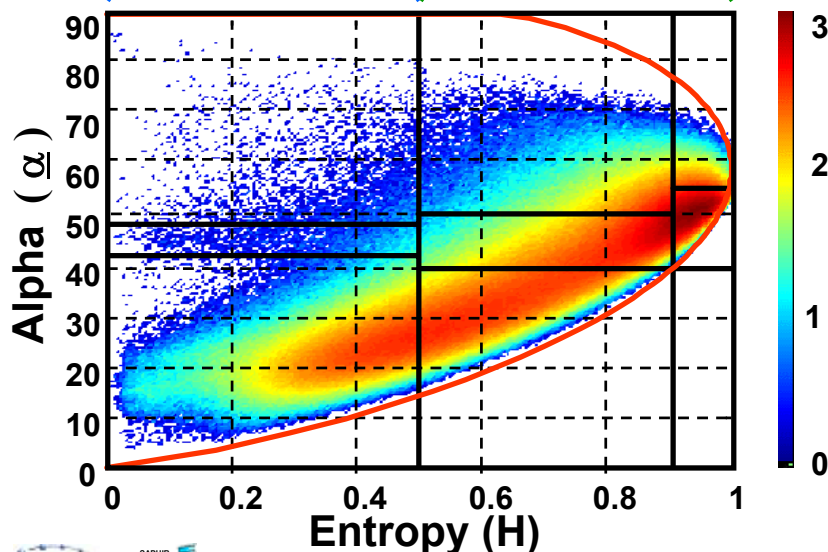


**A > 0.5**  
 $\lambda_2 \gg \lambda_3$

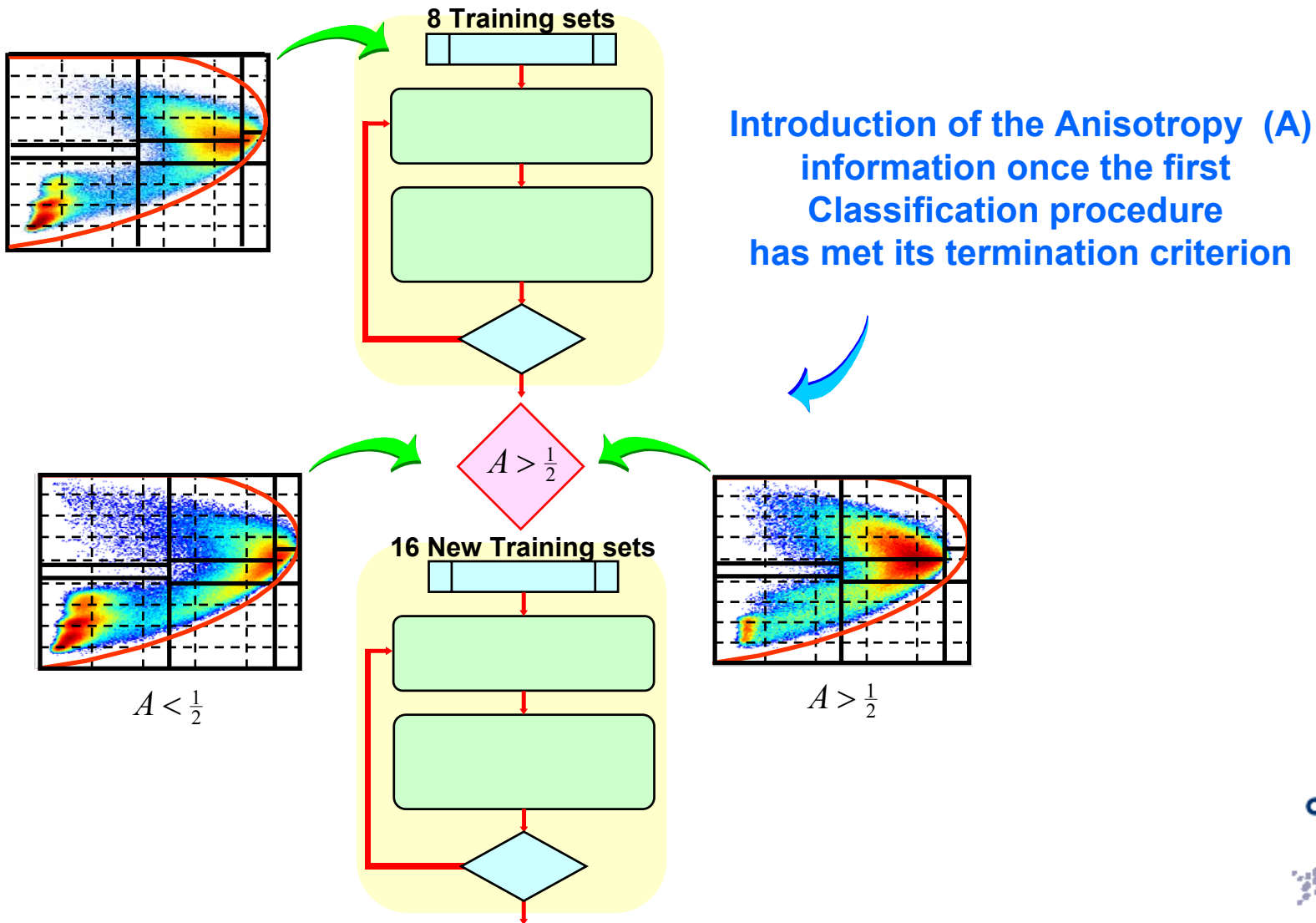
**1 SCATTERING MECHANISM**

**3 SCATTERING MECHANISMS**

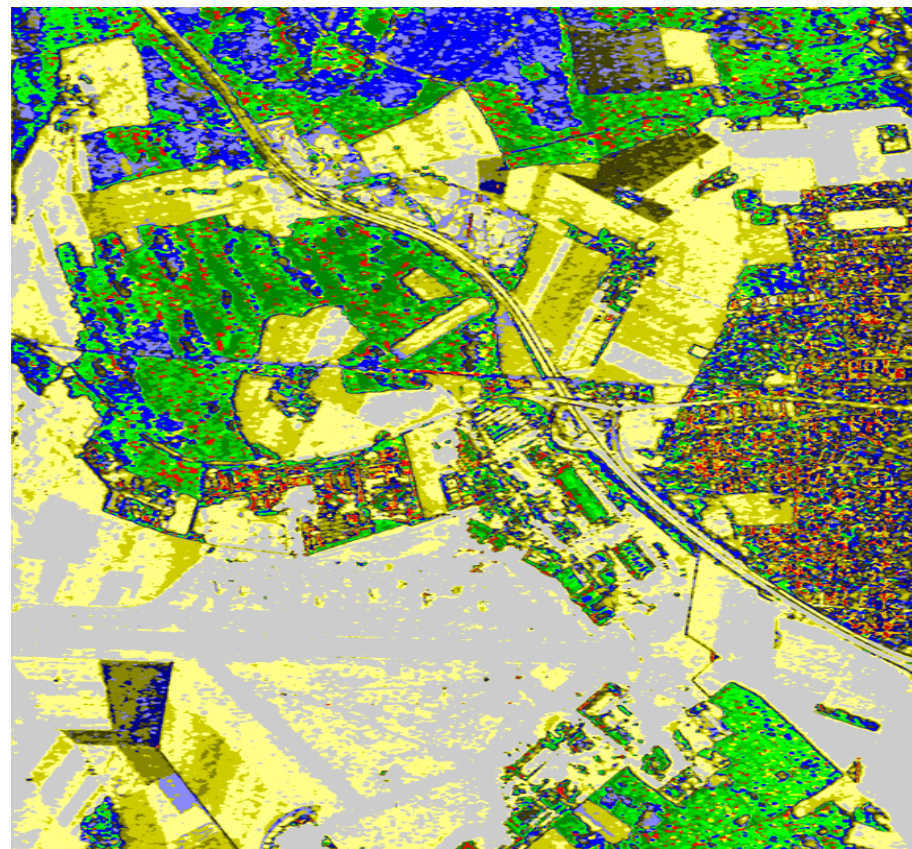
**2 SCATTERING MECHANISMS**  
( $1+\epsilon$ )      ( $\epsilon+\epsilon$ )



## 2 Successive k - mean Classification procedures



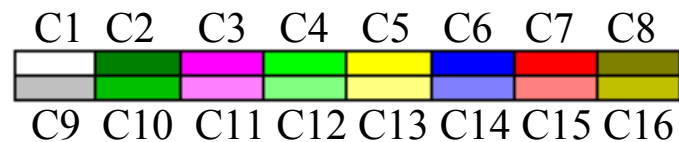
## Wishart H-A- $\alpha$ segmentation



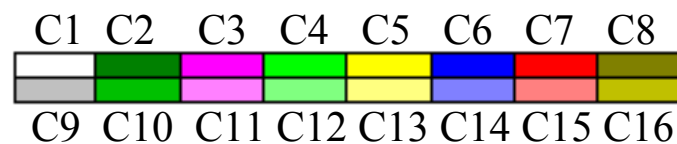
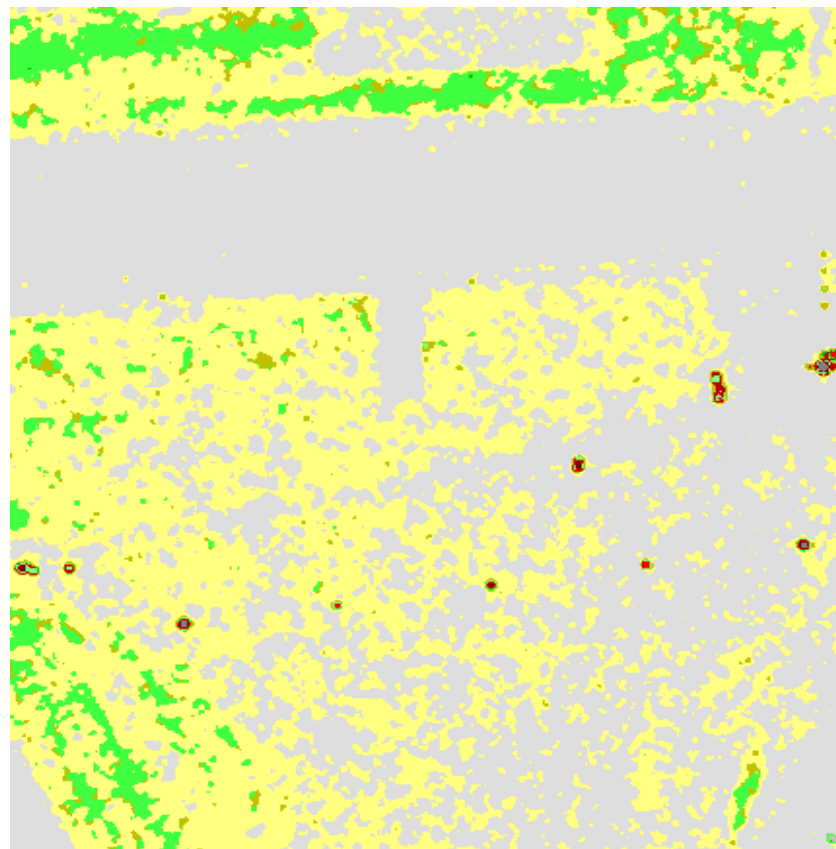
$2A_0$

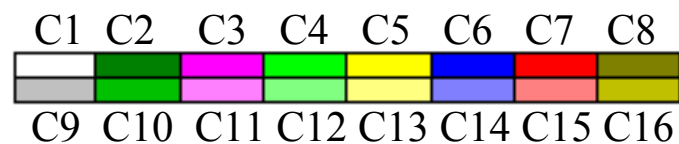
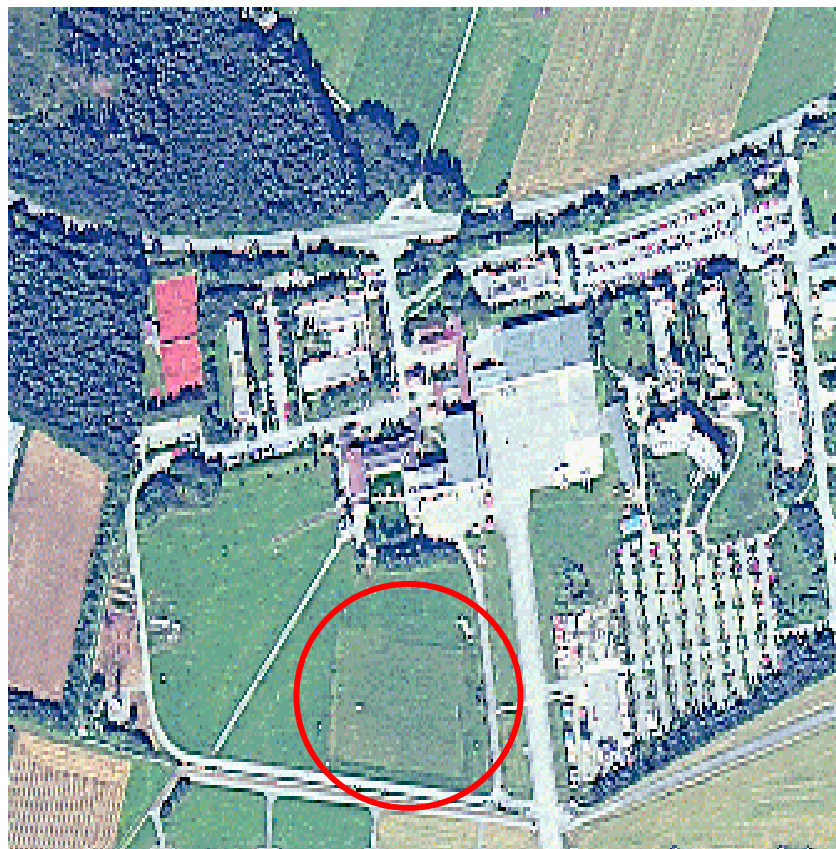
$B_0 + B$

$B_0 - B$





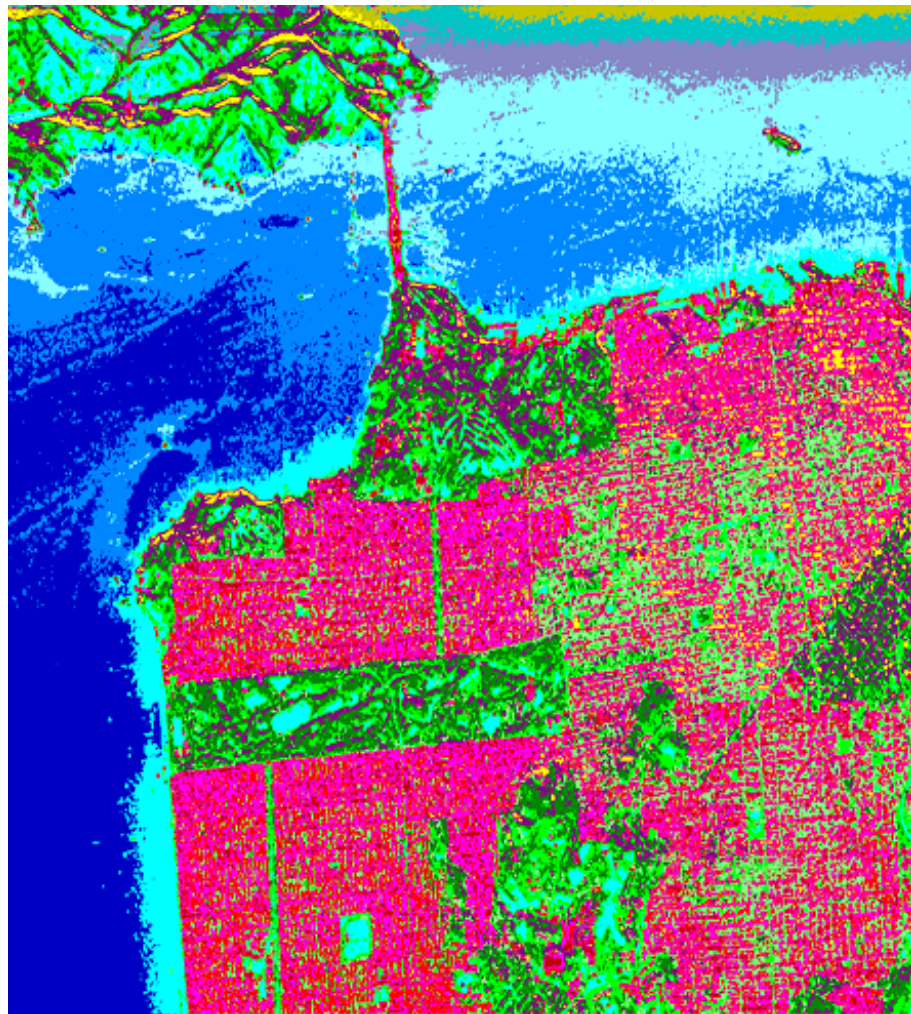




SAN FRANCISCO BAY JPL - AIRSAR L-band 1988



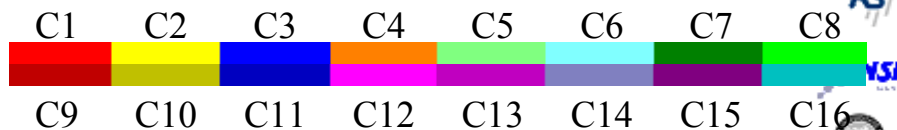
4th ITERATION



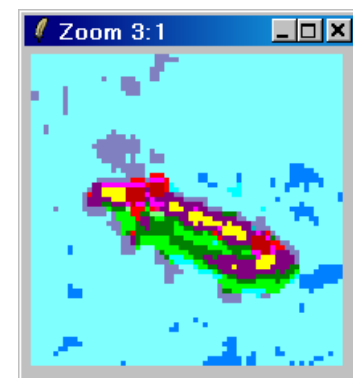
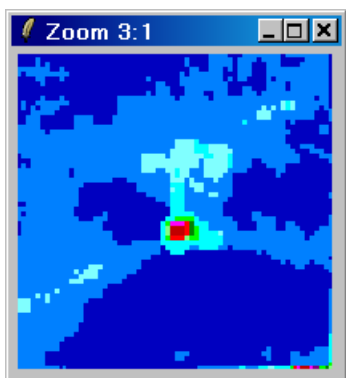
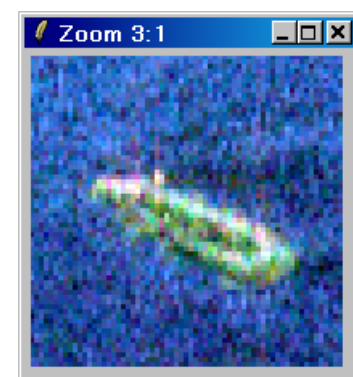
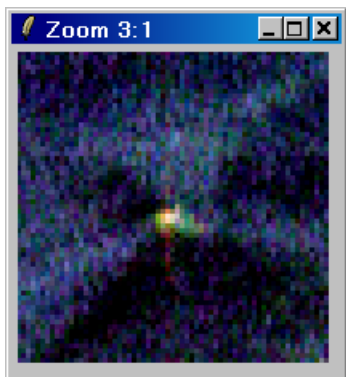
$2A_0$

$B_0 + B$

$B_0 - B$



SAN FRANCISCO BAY JPL - AIRSAR L-band 1988

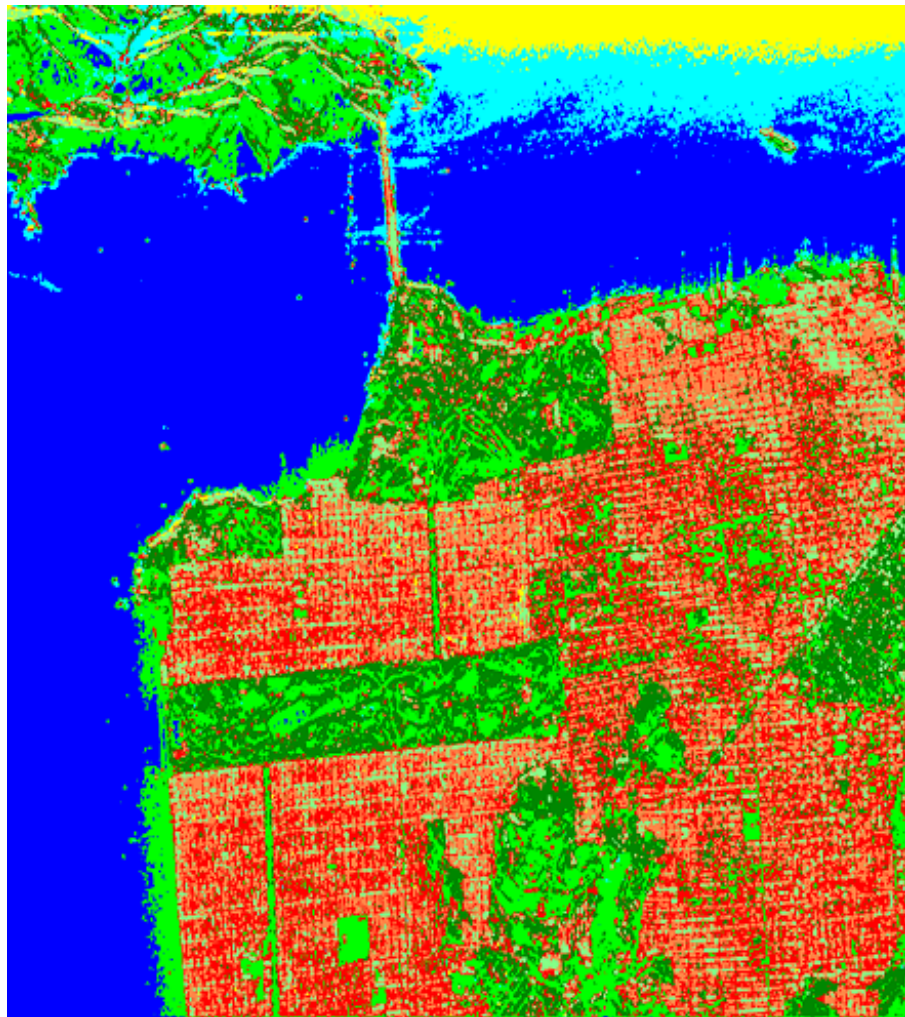


$$2A_0$$

$$B_0 + B$$

$$B_0 - B$$

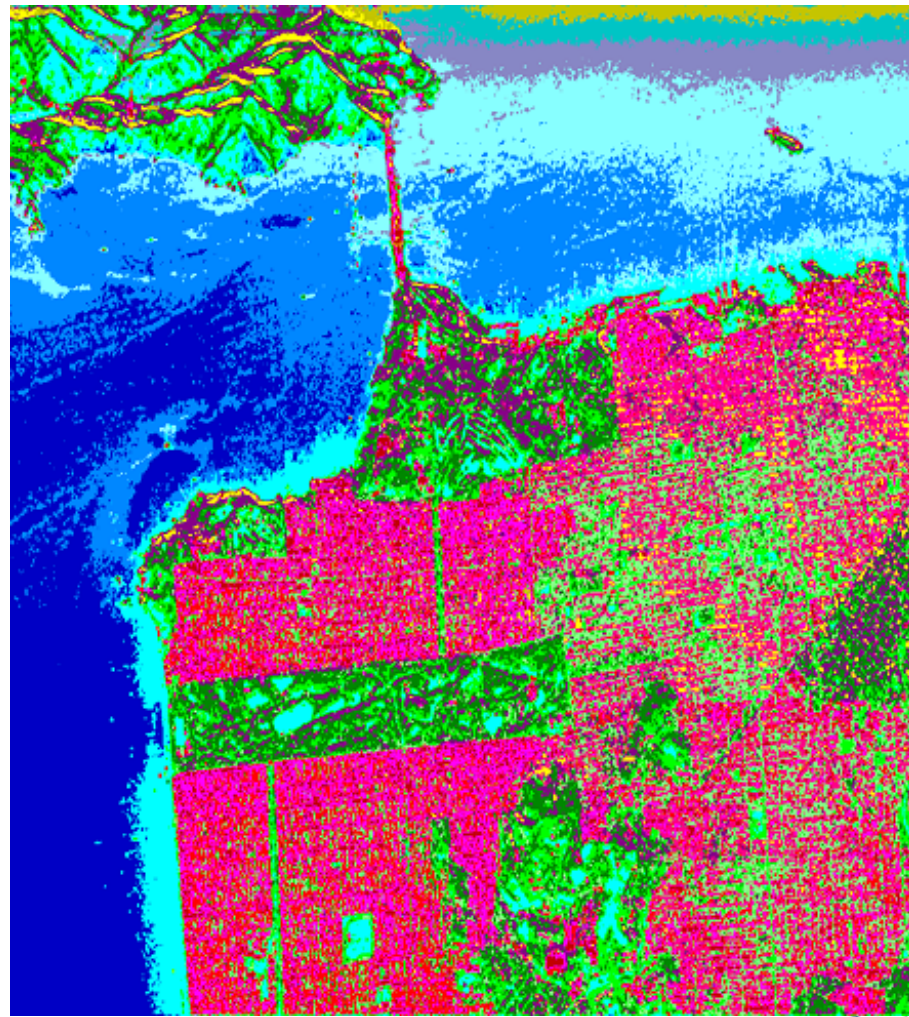
H /  $\alpha$  and WISHART CLASSIFIER




C1 C2 C3 C4 C5 C6 C7 C8




H / A /  $\alpha$  and WISHART CLASSIFIER



C1 C2 C3 C4 C5 C6 C7 C8

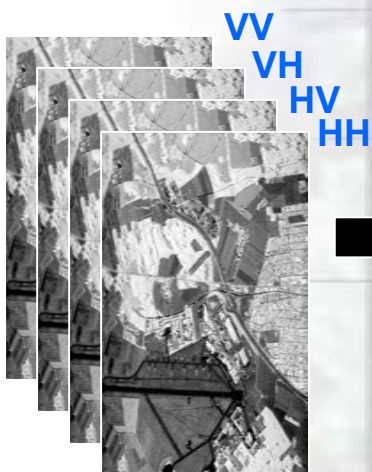


C9 C10 C11 C12 C13 C14 C15 C16



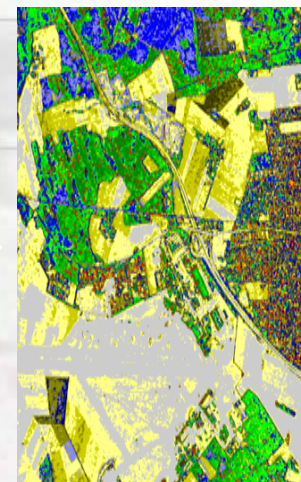
WISHART PDF

$$P(\langle [T] \rangle / [T_m]) = \frac{L^p \|\langle [T] \rangle\|^{L-p} e^{-L \text{Tr}([T_m]^{-1} \langle [T] \rangle)}}{\pi^{\frac{p(p-1)}{2}} \Gamma(L) \dots \Gamma(L-p+1) [T_m]^L}$$



## UNSUPERVISED POLARSAR CLASSIFICATION

E.POTTIER, J.S LEE (2000)



## Unsupervised Classification Preserving Scattering Mechanisms

J.S. Lee, M.R. Grunes, E. Pottier and L. Ferro-Famil, "Segmentation of polarimetric SAR images that preserves scattering mechanisms" Proceedings of EUSAR2002

## – Polarimetric SAR (POLSAR) classification

- Complex Wishart distribution (Lee et al., 1994)
- Wishart + Entropy/Alpha (Lee et al., 1999)
- Wishart + Entropy/Alpha/Anisotropy (Pottier and Lee, 2000)
- Deficiency: Wishart classifier is a statistic operator. Pixels in a class can be mixed in scattering mechanisms

## – A new approach

- Preserving scattering property of each pixel based on Freeman and Durden decomposition:
  - Double bounce
  - Surface
  - Volume (Canopy)
- Better stability in convergence
- Automated color rendering

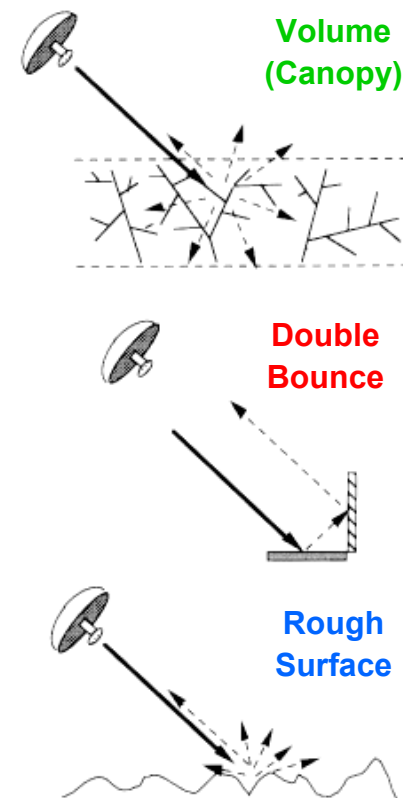
Courtesy of Dr J.S Lee



$|HH-VV|$ ,  $|HV|$ ,  $|HH+VV|$

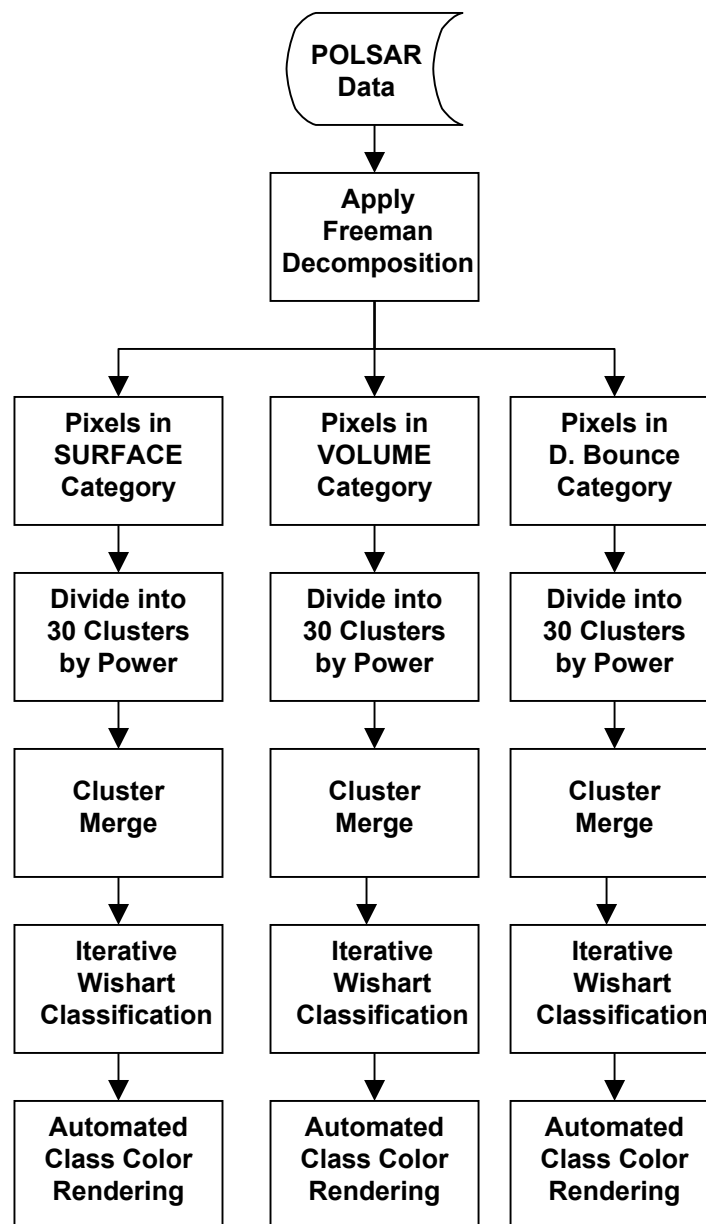


Freeman and Durden



A. Freeman and S.L. Durden, "A Three-Component Scattering Model for Polarimetric SAR Data" IEEE TGRS, vol. 36, no. 3, May 1998





## Wishart Iteration – After Class Merge

### Classification Maps



First Iteration



Second Iteration



Third Iteration

**Note: Stability insures good convergence**

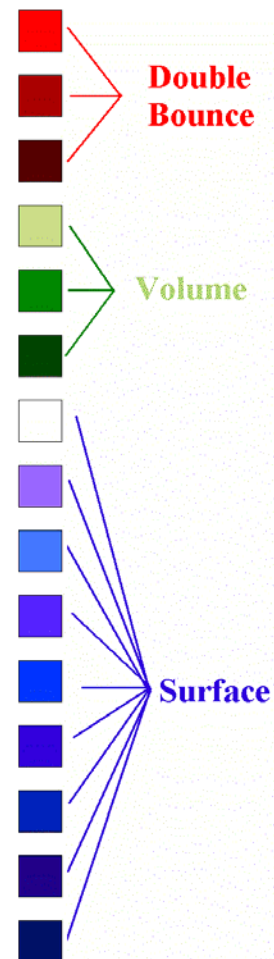
Courtesy of Dr J.S Lee



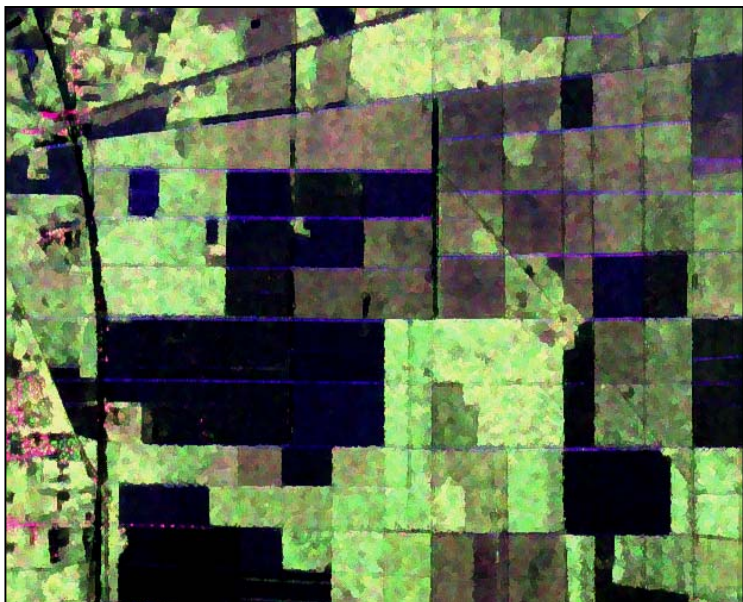
$|HH-VV|$ ,  $|HV|$ ,  $|HH+VV|$



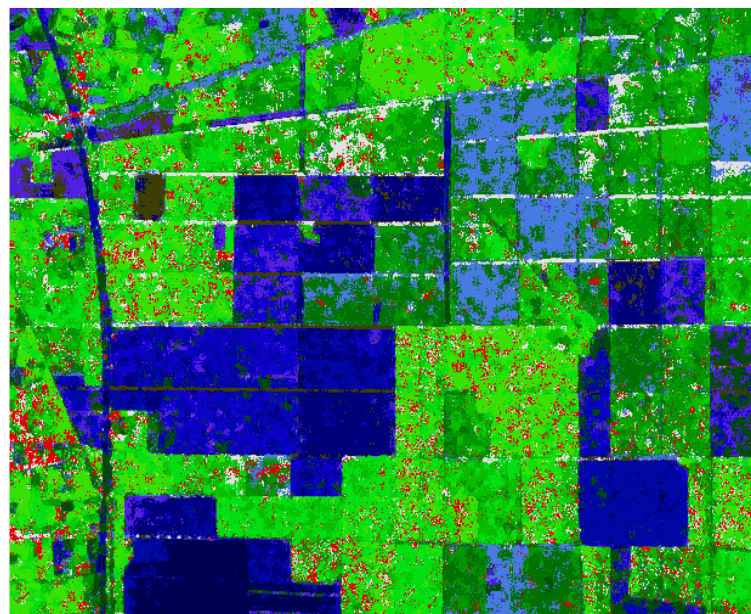
4<sup>th</sup> Iteration (15 classes)



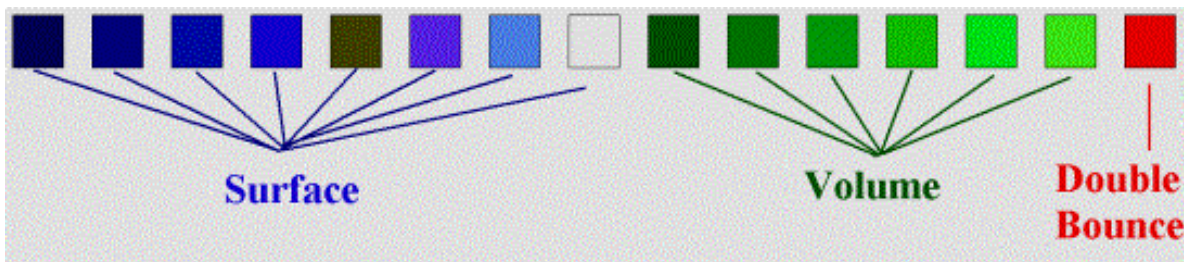
Courtesy of Dr J.S Lee



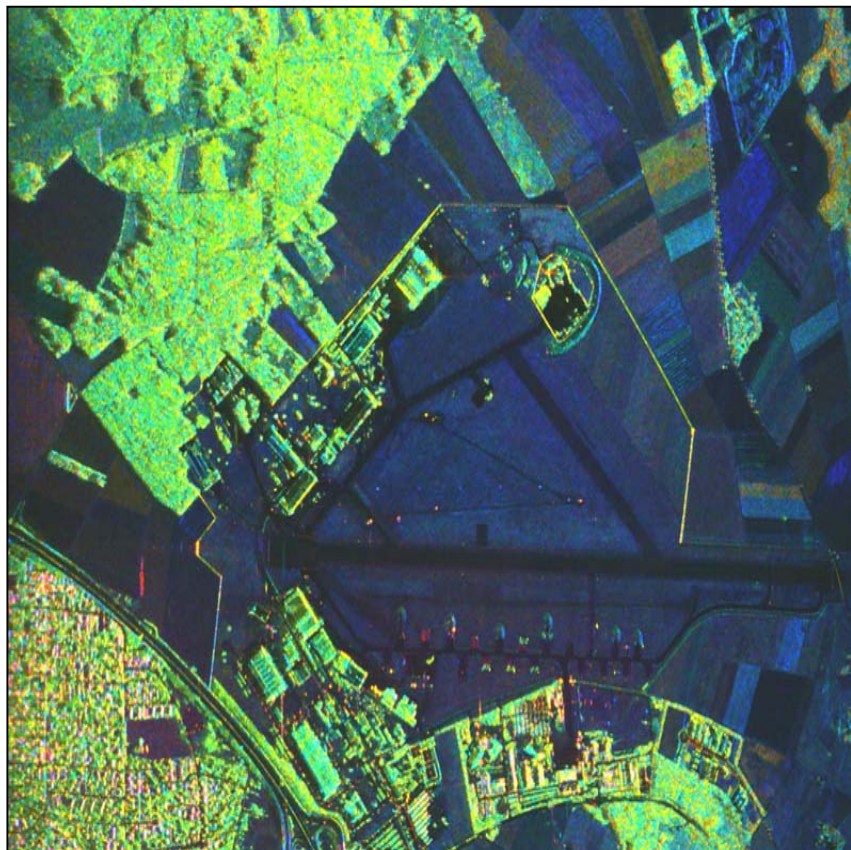
$|HH-VV|$ ,  $|HV|$ ,  $|HH+VV|$



4<sup>th</sup> Iteration (15 classes)



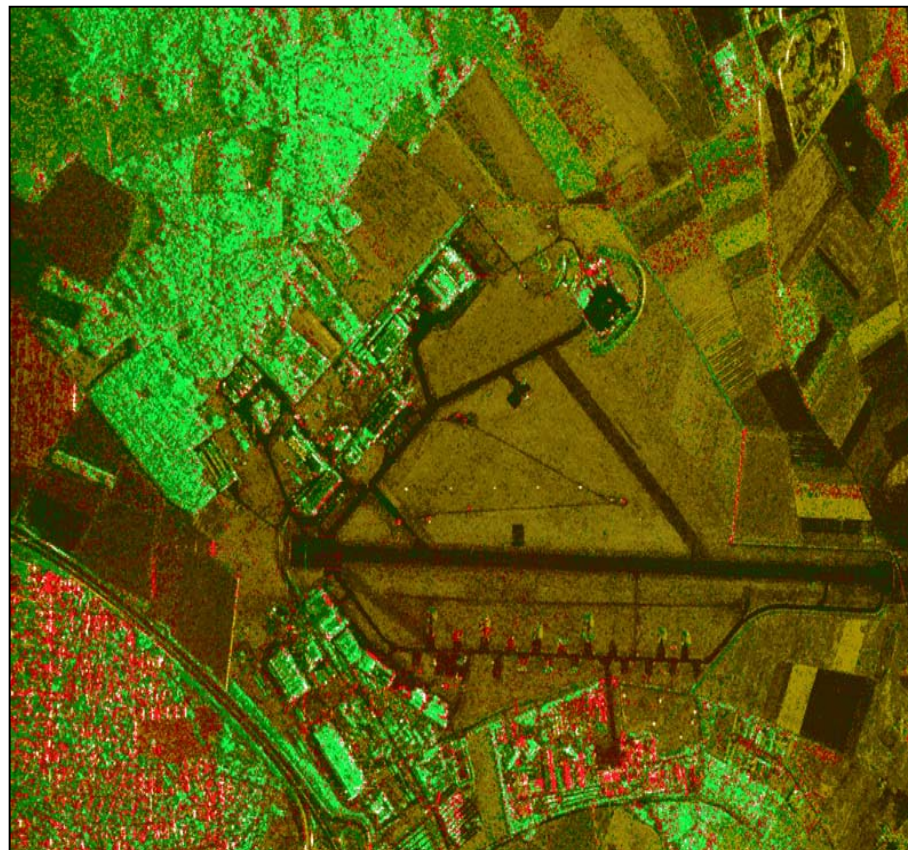
Courtesy of Dr J.S Lee



$2A_0$

$B_0 + B$

$B_0 - B$



4<sup>th</sup> Iteration (15 classes)

