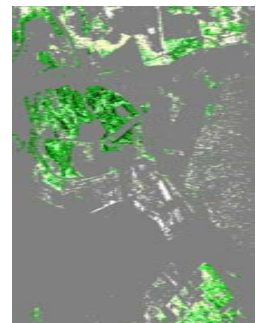
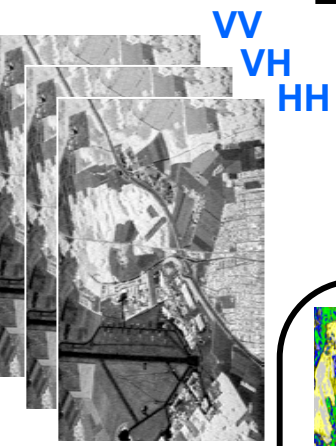
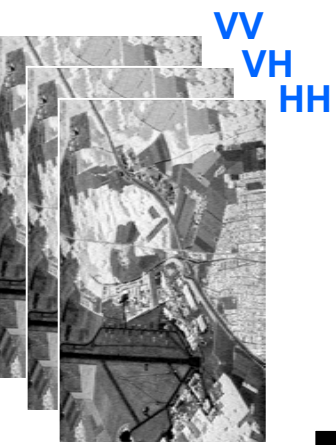


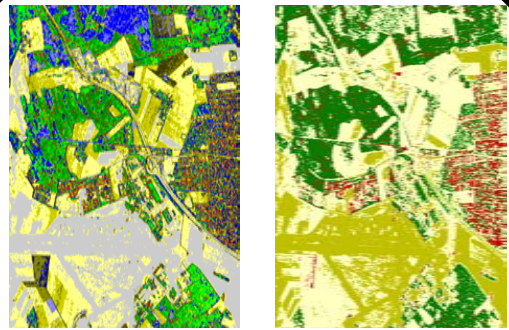
POL-IN-SAR CLASSIFICATION

WISHART PDF
$$P(\langle [T] \rangle / [T_m]) = \frac{L^{Lp} \langle [T] \rangle^{L-p} e^{-LTr([T_m] \Gamma^{-1} \langle [T] \rangle)}}{\pi^{\frac{p(p-1)}{2}} \Gamma(L) \dots \Gamma(L-p+1) [T_m]^L}$$


POLINSAR CLASSIFICATION
 L. FERRO-FAMIL, E.POTTIER, J.S LEE (2002)



POLSAR CLASSIFICATION



OPTIMUM INTERFEROMETRIC COHERENCES SPECTRUM



POLSAR



INSAR



**POL-IN-SAR
CLASSIFICATION**

POLINSAR – WISHART CLASSIFIER

L. Ferro-Famil, E. Pottier, J.S. Lee (2001-2002)





POL-SAR INFORMATION

**DLR E-SAR L Band
In-Pol SAR (1.5m x 3m) – Baseline 5m**



IN-SAR INFORMATION

COMPLEMENTARY INFORMATION

γ



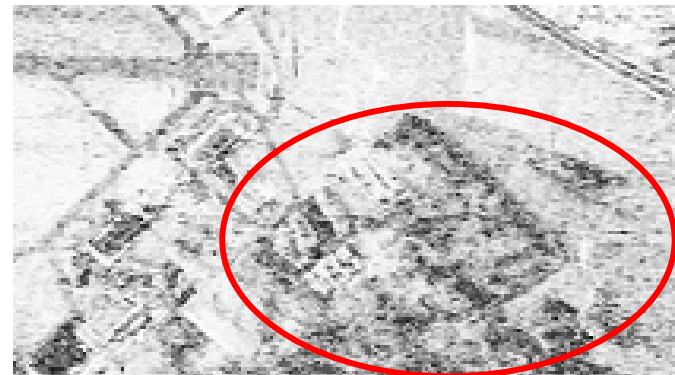
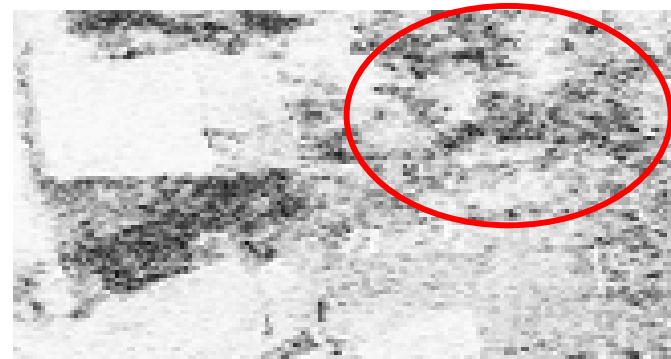
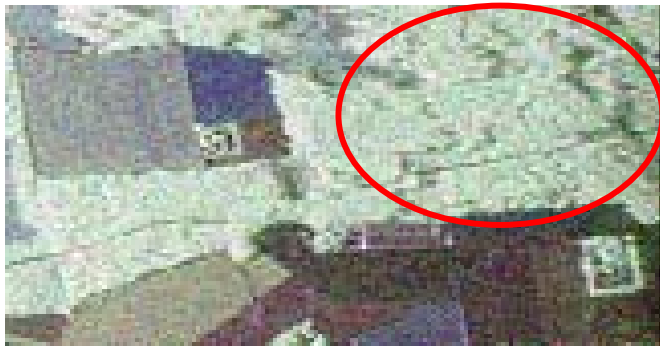
HETEROGENEOUS AREA

**DIFFERENT POLARIMETRIC
SCATTERING MECHANISMS**



HOMOGENEOUS AREA

**CONSTANT INTERFEROMETRIC
COHERENCE**

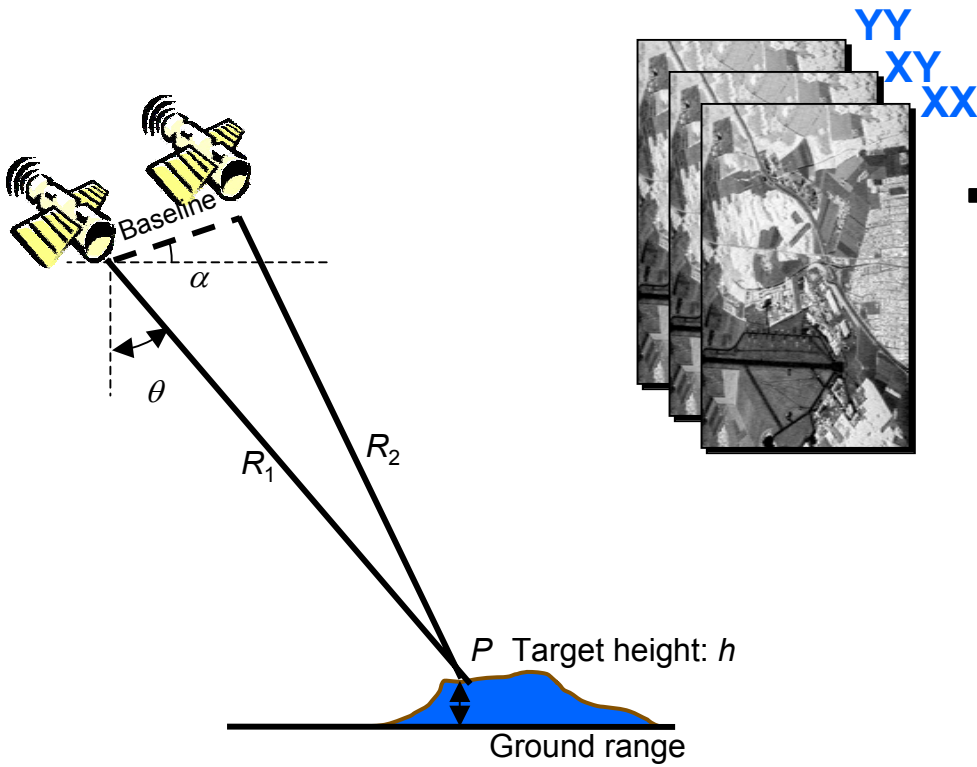


HOMOGENEOUS AREA

HETEROGENEOUS AREA

**SAME POLARIMETRIC
SCATTERING MECHANISMS**

**DIFFERENT INTERFEROMETRIC
COHERENCE**



$$\underline{k}_1 = \frac{1}{\sqrt{2}} \begin{bmatrix} S_{XX_1} + S_{YY_1} \\ S_{XX_1} - S_{YY_1} \\ 2S_{XY_1} \end{bmatrix}$$

$\underline{k} = \begin{bmatrix} \underline{k}_1 \\ \underline{k}_2 \end{bmatrix}$ **POLARIMETRIC INTERFEROMETRIC TARGET VECTOR**



$$\underline{k}_2 = \frac{1}{\sqrt{2}} \begin{bmatrix} S_{XX_2} + S_{YY_2} \\ S_{XX_2} - S_{YY_2} \\ 2S_{XY_2} \end{bmatrix}$$

$$\underline{\underline{k}} = \begin{bmatrix} \underline{k}_1 \\ \underline{k}_2 \end{bmatrix} \quad \text{POLARIMETRIC INTERFEROMETRIC TARGET VECTOR}$$



$$\langle [T_6] \rangle = \langle \underline{\underline{k}} \cdot \underline{\underline{k}}^{T*} \rangle = \begin{bmatrix} \langle \underline{k}_1 \cdot \underline{k}_1^{T*} \rangle & \langle \underline{k}_1 \cdot \underline{k}_2^{T*} \rangle \\ \langle \underline{k}_2 \cdot \underline{k}_1^{T*} \rangle & \langle \underline{k}_2 \cdot \underline{k}_2^{T*} \rangle \end{bmatrix} = \begin{bmatrix} \langle [T_1] \rangle & \langle [\Omega_{12}] \rangle \\ \langle [\Omega_{12}]^{T*} \rangle & \langle [T_2] \rangle \end{bmatrix}$$

POLARIMETRIC INTERFEROMETRIC COHERENCY MATRIX (6x6)

$\langle [T_1] \rangle$ HERMITIAN POLARIMETRIC COHERENCY MATRIX (3x3)

$\langle [T_2] \rangle$ HERMITIAN POLARIMETRIC COHERENCY MATRIX (3x3)

$\langle [\Omega_{12}] \rangle$ NON HERMITIAN POLARIMETRIC INTER-COHERENCY MATRIX (3x3)

POLSAR IMAGES $I_1 = \underline{w}_1^{T*} \cdot \underline{k}_1$ and $I_2 = \underline{w}_2^{T*} \cdot \underline{k}_2$

With: $(\underline{w}_1, \underline{w}_2)$ **Complex Unitary Vectors**



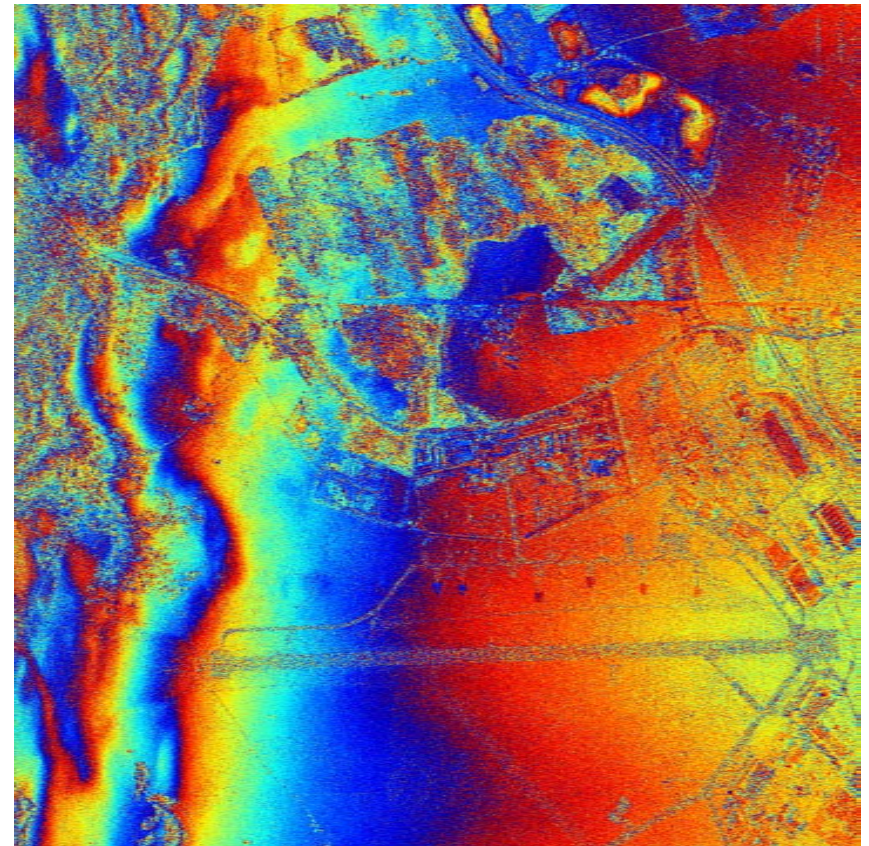
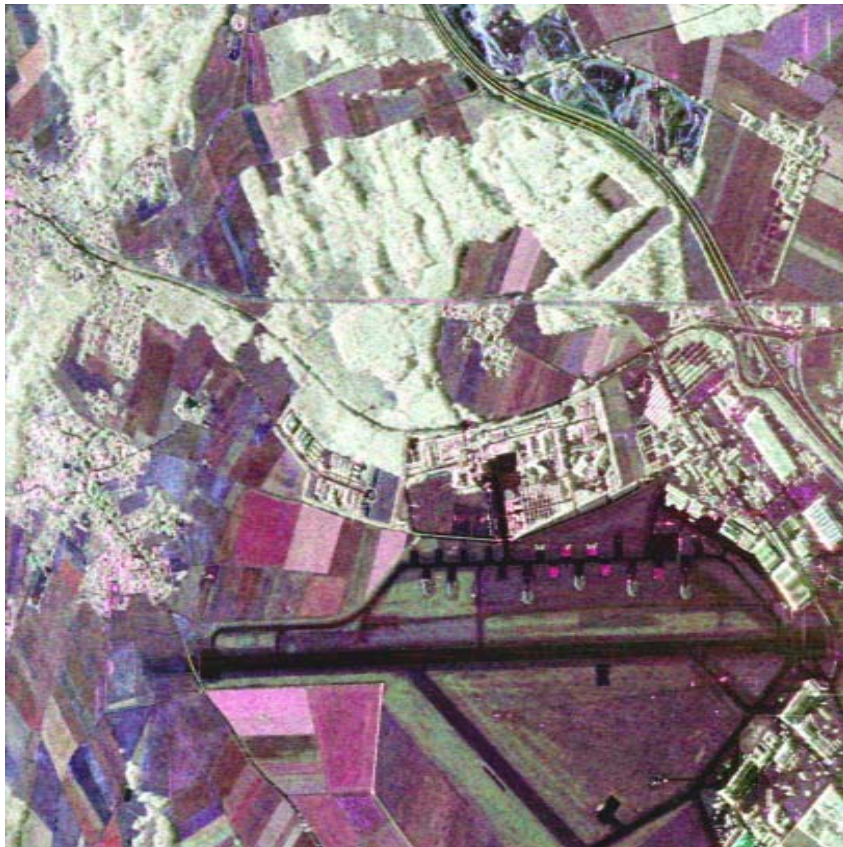
$$\gamma(\underline{w}_1, \underline{w}_2) = \frac{\langle I_1 I_2^* \rangle}{\sqrt{\langle I_1 I_1^* \rangle \langle I_2 I_2^* \rangle}} = \frac{\langle \underline{w}_1 [\Omega_{12}] \underline{w}_2^{T*} \rangle}{\sqrt{\langle \underline{w}_1 [T_1] \underline{w}_1^{T*} \rangle \langle \underline{w}_2 [T_2] \underline{w}_2^{T*} \rangle}}$$

COMPLEX POLARIMETRIC INTERFEROMETRIC COHERENCE

$\arg(\gamma)$ **INTERFEROMETRIC PHASE**

$|\gamma|$ **CROSS-CORRELATION COEFFICIENT**

$$\gamma = \gamma_{SNR} \cdot \gamma_{spatial} \cdot \gamma_{temporal} \cdot \gamma_{polar}$$



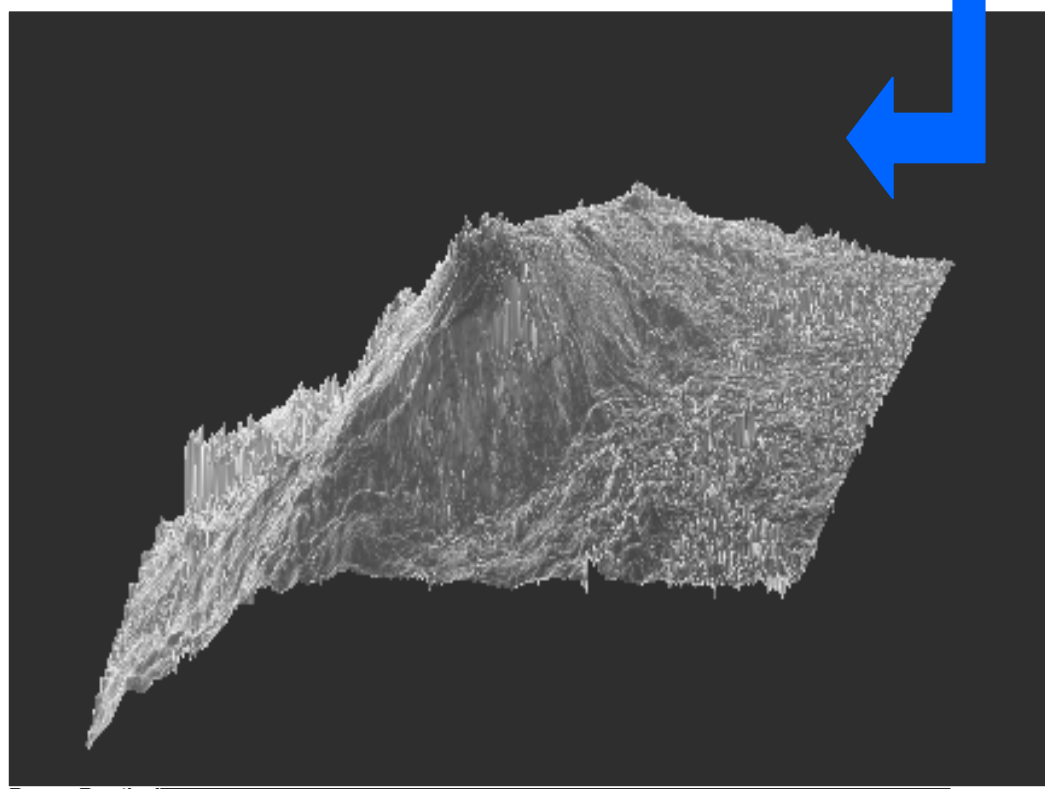
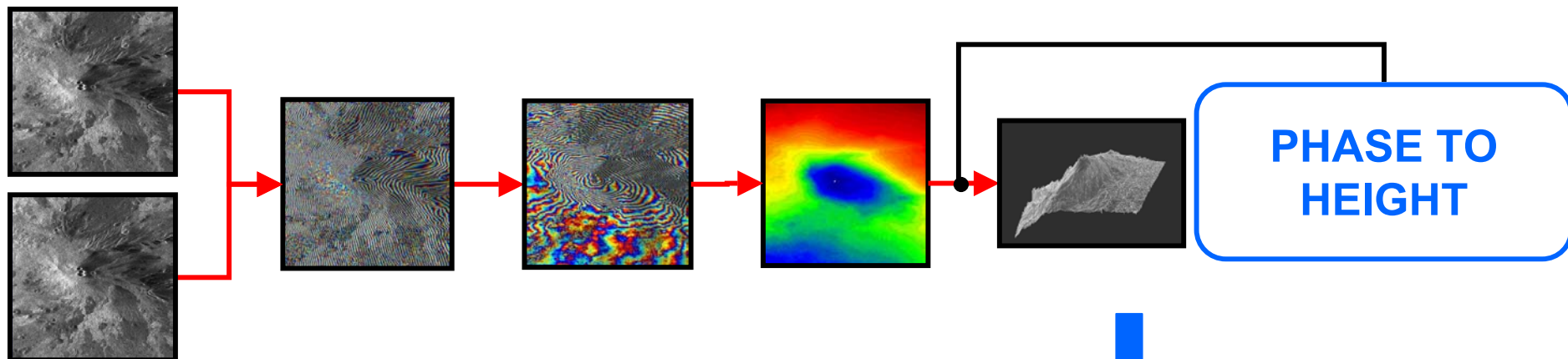
DLR E-SAR L Band
In-Pol SAR (1.5m x 3m) – Baseline 5m

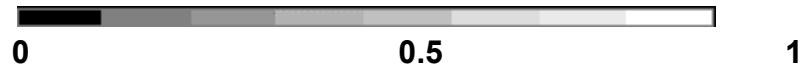


POL-SAR INFORMATION

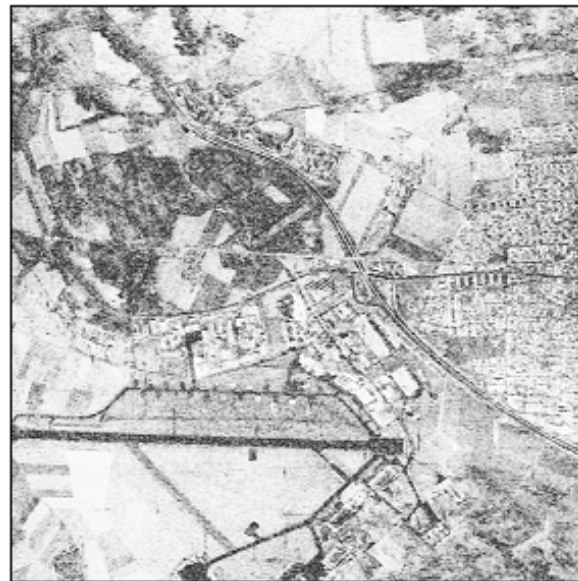


IN-SAR INFORMATION γ

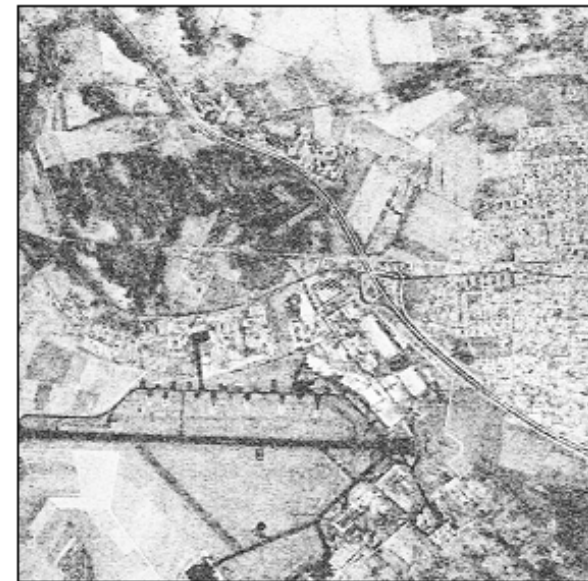




$\gamma_{HH_1-HH_2}$



$\gamma_{HV_1-HV_2}$



$\gamma_{VV_1-VV_2}$

$$\downarrow$$

$$\underline{w}_1 = \underline{w}_2 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix}$$

$$\downarrow$$

$$\underline{w}_1 = \underline{w}_2 = \begin{bmatrix} 0 \\ 0 \\ \sqrt{2} \end{bmatrix}$$

$$\downarrow$$

$$\underline{w}_1 = \underline{w}_2 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ -1 \\ 0 \end{bmatrix}$$

$$\gamma = \gamma_{SNR} \cdot \gamma_{spatial} \cdot \gamma_{temporal} \cdot \gamma_{polar}$$

$$\gamma(\underline{w}_1, \underline{w}_2) = \frac{\langle \underline{I}_1 \underline{I}_2^* \rangle}{\sqrt{\langle \underline{I}_1 \underline{I}_1^* \rangle \langle \underline{I}_2 \underline{I}_2^* \rangle}} = \frac{\langle \underline{w}_1 [\underline{\Omega}_{12}] \underline{w}_2^{T*} \rangle}{\sqrt{\langle \underline{w}_1 [\underline{T}_1] \underline{w}_1^{T*} \rangle \langle \underline{w}_2 [\underline{T}_2] \underline{w}_2^{T*} \rangle}}$$

COMPLEX POLARIMETRIC INTERFEROMETRIC COHERENCE



**QUESTION: WHICH POLARISATION COMBINATION LEADS TO THE
MAXIMUM POSSIBLE INTERFEROMETRIC COHERENCE ?**



**POLARIMETRIC INTERFEROMETRIC COHERENCE
OPTIMISATION PROCEDURE**

S.R CLOUDE – K. PAPATHANASSIOU (1999)

POLARIMETRIC INTERFEROMETRIC COHERENCE OPTIMISATION PROCEDURE

S.R. CLOUDE – K. PAPATHANASSIOU (1999)

$$[T_1]^{-1} [\Omega_{12}] [T_2]^{-1} [\Omega_{12}]^{T*} \underline{w}_1 = [A][B] \underline{w}_1 = \lambda_1 \lambda_2^* \underline{w}_1 = \nu \underline{w}_1$$

$$[T_2]^{-1} [\Omega_{12}]^{T*} [T_1]^{-1} [\Omega_{12}] \underline{w}_2 = [B][A] \underline{w}_2 = \lambda_1 \lambda_2^* \underline{w}_2 = \nu \underline{w}_2$$

$[T_2]^{-1} [\Omega_{12}]^{T*} [T_1]^{-1} [\Omega_{12}]$ is not hermitian but $\nu = \lambda_1 \lambda_2^*$ are real



3 Real Eigenvalues: $\nu_1 \geq \nu_2 \geq \nu_3 \geq 0$

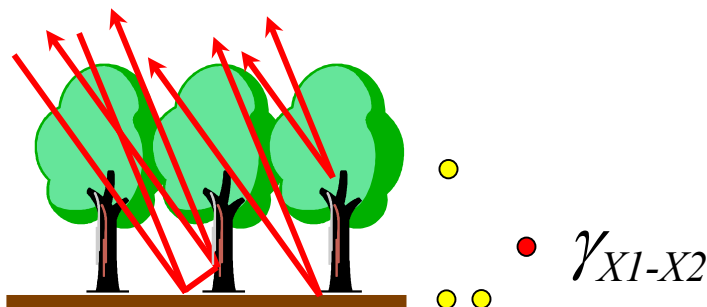
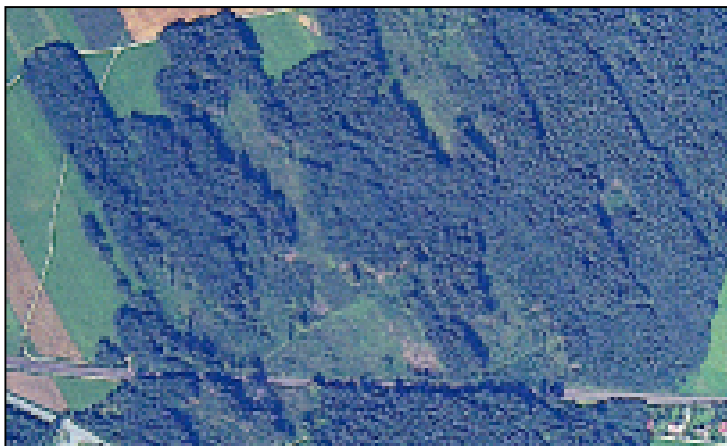
3 Pairs of Eigenvectors: $\{\underline{w}_{11}, \underline{w}_{21}\}, \{\underline{w}_{12}, \underline{w}_{22}\}, \{\underline{w}_{13}, \underline{w}_{23}\}$



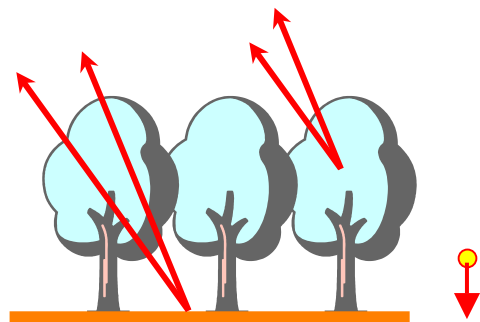
Optimum Coherence Values: $\gamma_i = \sqrt{\nu_i}$

Optimum Scattering Mechanisms: $\{\underline{w}_{1i}, \underline{w}_{2i}\}$

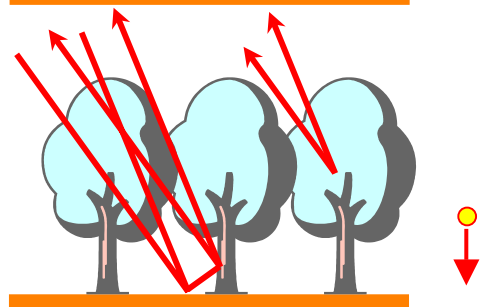
PHYSICAL INTERPRETATION OF POLARIMETRIC INTERFEROMETRIC COHERENCES OPTIMISATION ALGORITHM



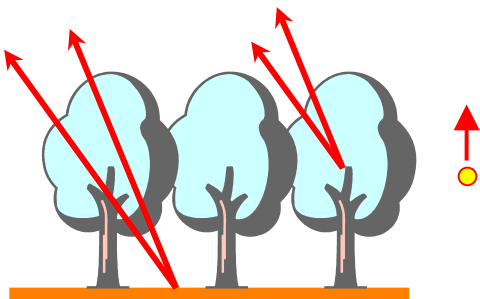
$$\{\underline{w}_{11}, \underline{w}_{21}\}$$



$$\{\underline{w}_{12}, \underline{w}_{22}\}$$



$$\{\underline{w}_{13}, \underline{w}_{23}\}$$



IN AN OPTIMISED WORLD



γ_{opt1}



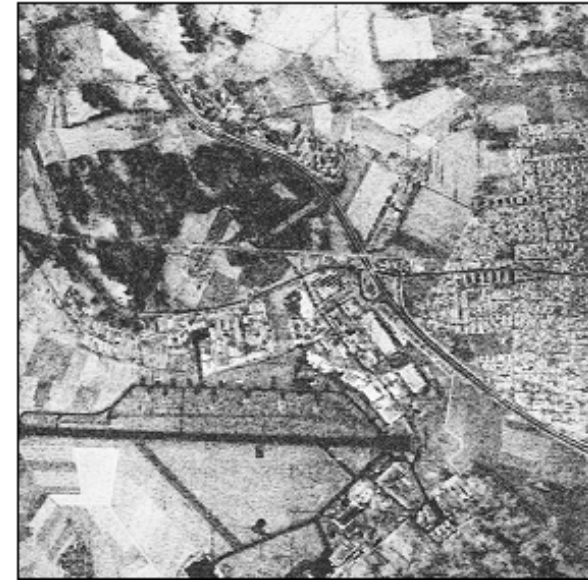
$\{\underline{w}_{11}, \underline{w}_{21}\}$



γ_{opt2}



$\{\underline{w}_{12}, \underline{w}_{22}\}$



γ_{opt3}



$\{\underline{w}_{13}, \underline{w}_{23}\}$

Optimum coherences spectrum $(\gamma_{opt1}, \gamma_{opt2}, \gamma_{opt3})$

Independent of the radar polarization basis



$|\gamma_{opt1}|$

$|\gamma_{opt2}|$

$|\gamma_{opt3}|$

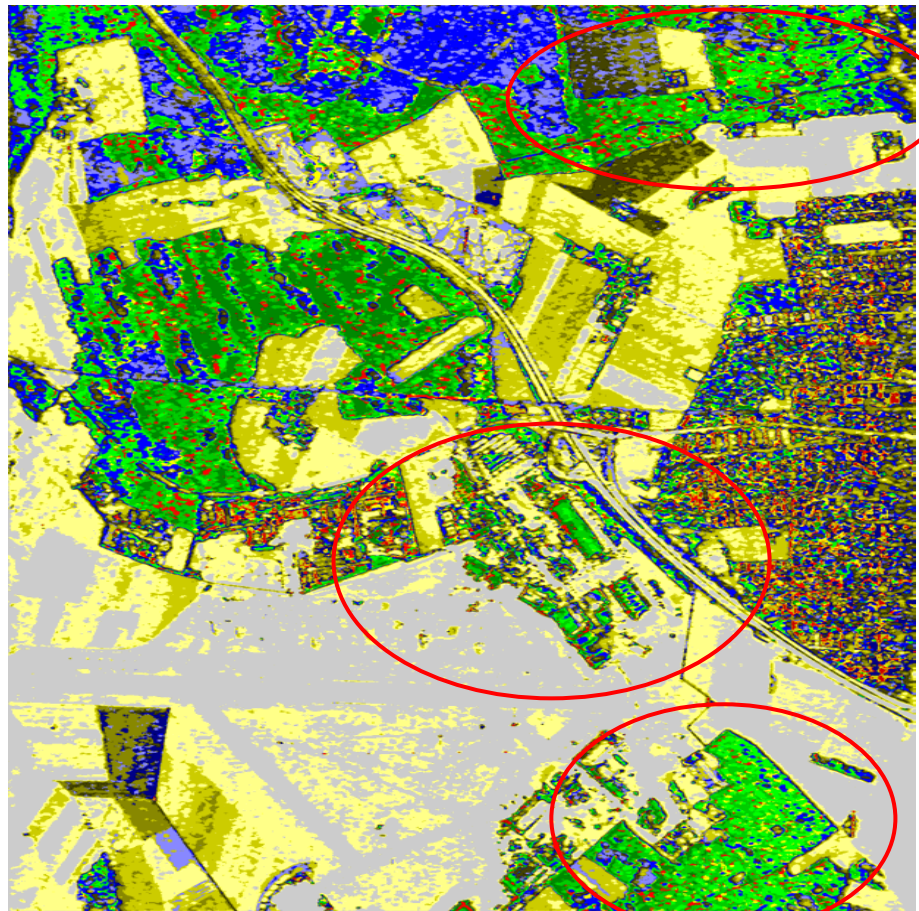


$2A_0$

$B_0 + B$

$B_0 - B$ CRS

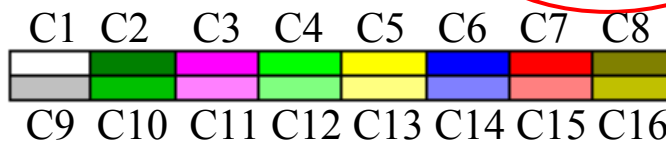
Wishart H-A- α segmentation



$|\gamma_{opt1}|$

$|\gamma_{opt2}|$

$|\gamma_{opt3}|$



ANALYSIS OF THE OPTIMUM COHERENCES SPECTRUM



INTERFEROMETRIC COHERENCES SPECTRUM SEGMENTATION PROCEDURE

Information about the coherent scattering mechanisms

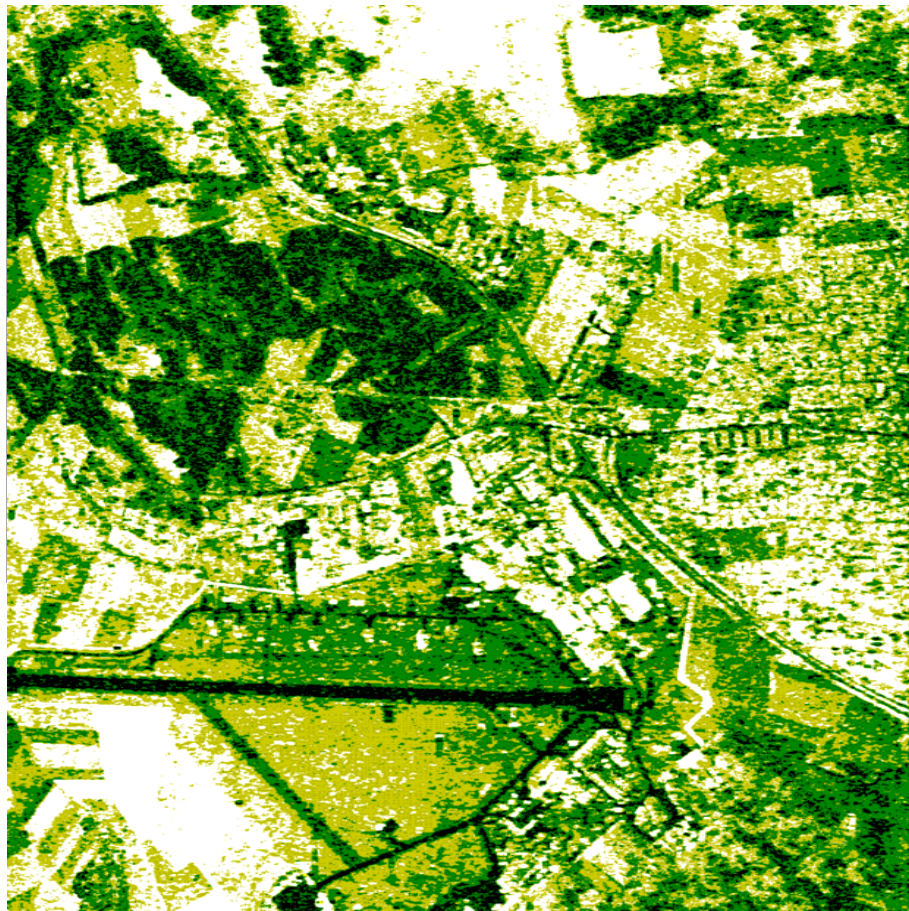
SPECTRUM DESCRIPTORS

$$A_1 = \frac{\tilde{\gamma}_{opt 1} - \tilde{\gamma}_{opt 2}}{\tilde{\gamma}_{opt 1}} \quad A_2 = \frac{\tilde{\gamma}_{opt 1} - \tilde{\gamma}_{opt 3}}{\tilde{\gamma}_{opt 1}}$$

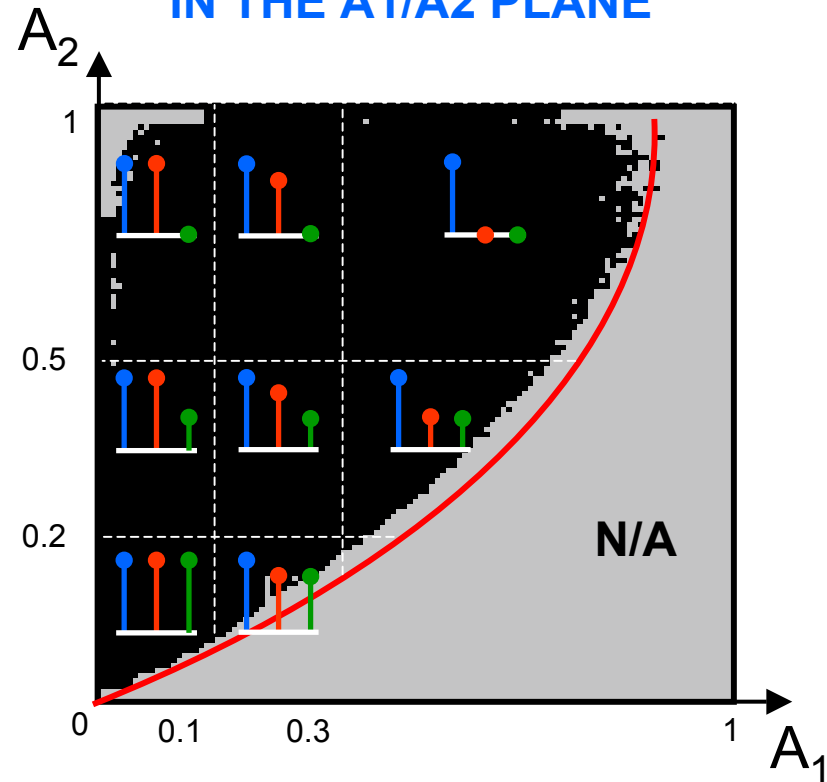
With :

$$\tilde{\gamma}_{opt i} = \frac{|\gamma_{opt i}|}{\sum_{j=1}^3 |\gamma_{opt j}|}$$

INTERFEROMETRIC COHERENCES SPECTRUM SEGMENTATION RESULTS



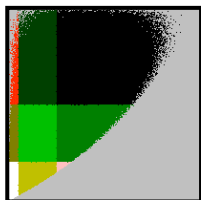
COHERENCES SPECTRUM DISTRIBUTION IN THE A1/A2 PLANE



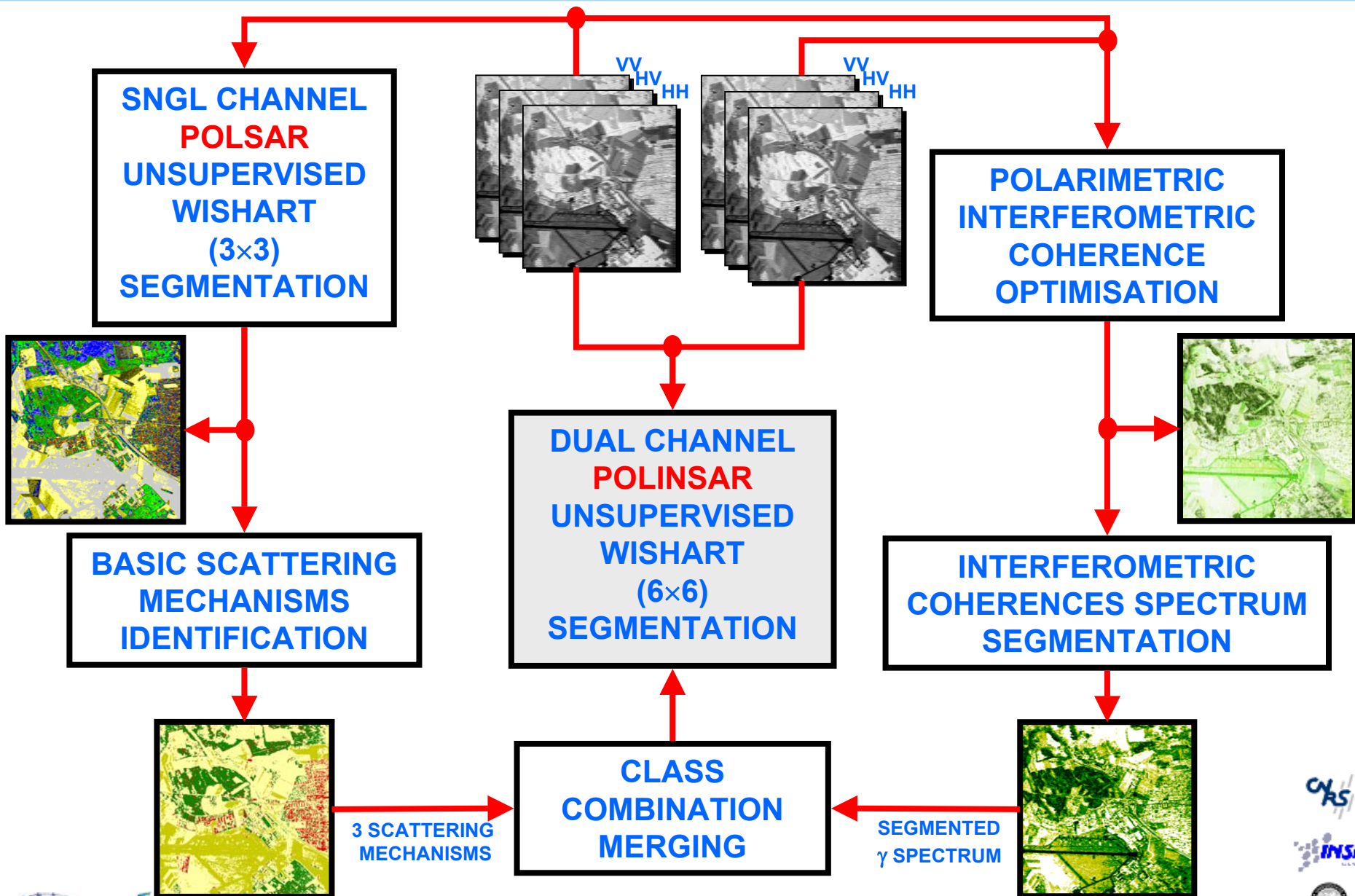
Fixed thresholds on A_1 , A_2



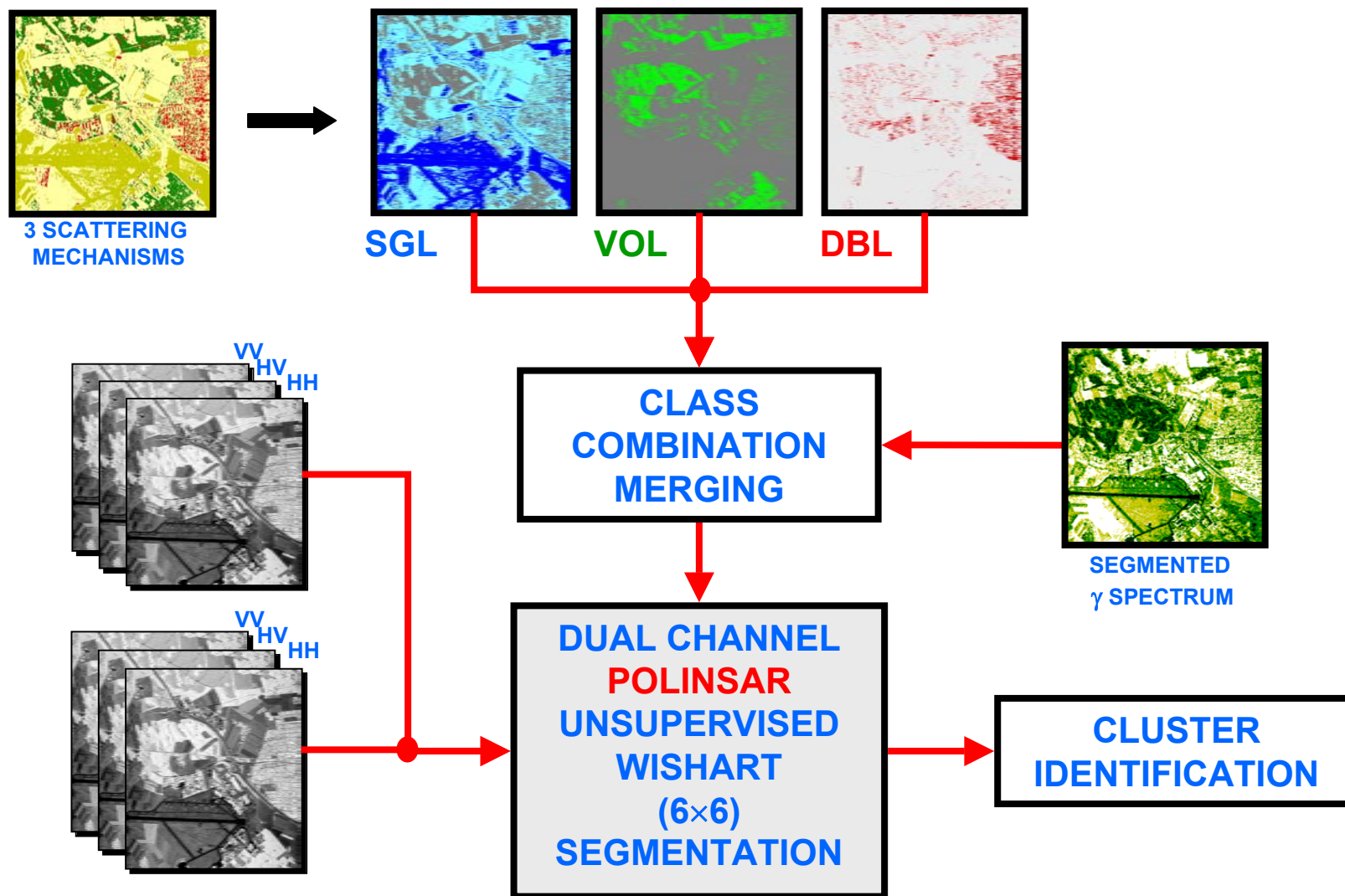
Interpretation of the
spectrum distribution
Number of coherent mechanisms



9 potential classes



SEGMENTATION OF EACH BASIC SCATTERING MECHANISM TYPE



DUAL CHANNELS POLINSAR UNSUPERVISED SEGMENTATION

$$\langle [T_6] \rangle = \langle \underline{k} \cdot \underline{k}^{T*} \rangle = \begin{bmatrix} \langle \underline{k}_1 \cdot \underline{k}_1^{T*} \rangle & \langle \underline{k}_1 \cdot \underline{k}_2^{T*} \rangle \\ \langle \underline{k}_2 \cdot \underline{k}_1^{T*} \rangle & \langle \underline{k}_2 \cdot \underline{k}_2^{T*} \rangle \end{bmatrix} = \begin{bmatrix} \langle [T_1] \rangle & \langle [\Omega_{12}] \rangle \\ \langle [\Omega_{12}]^{T*} \rangle & \langle [T_2] \rangle \end{bmatrix}$$

POLARIMETRIC INTERFEROMETRIC COHERENCY MATRIX (6x6)



$\langle [T_6] \rangle$ **FOLLOWS A WISHART DISTRIBUTION**

$$P(\langle [T_6] \rangle / [\Sigma_m]) = \frac{\| \langle [T_6] \rangle \|^{L-p} \exp(-tr([\Sigma_m]^{-1} \langle [T_6] \rangle))}{K(L, p) [\Sigma_m]^L} = W_C(L, [\Sigma_m])$$

L: Number of Look
p: Polarimetric Dimension

With: $K(L, p) = \frac{\pi^{\frac{p(p-1)}{2}}}{L^{Lp}} \Gamma(L) \dots \Gamma(L - p + 1)$

$[\Sigma_m]$: Cluster Center of the class m

BAYES MAXIMUM LIKELIHOOD CLASSIFICATION PROCEDURE

$$\langle [T_6] \rangle \in [\Sigma_m] \quad \text{if} \quad d_m(\langle [T_6] \rangle) < d_j(\langle [T_6] \rangle) \quad \forall j \neq m$$

With: $d(\langle [T_6] \rangle, [\Sigma_m]) = \ln |[\Sigma_m]| + \text{tr}([\Sigma_m]^{-1} \langle [T_6] \rangle)$

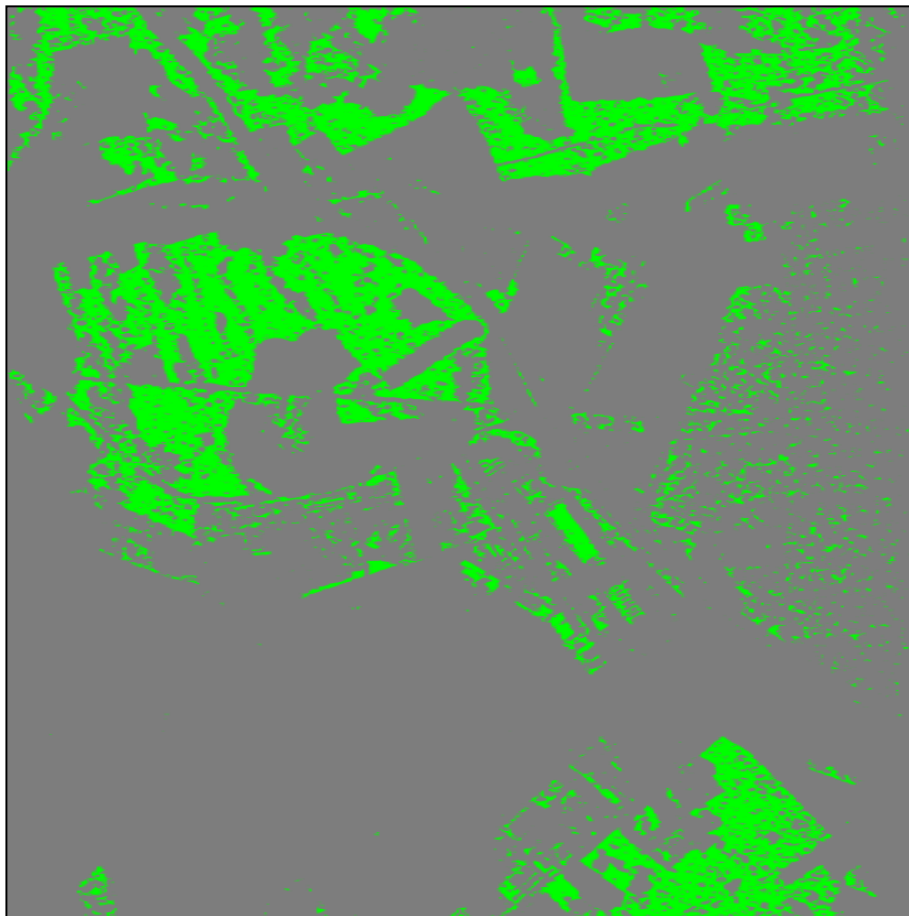
$[\Sigma_m]$: Cluster Center of the class m

Where: $[\Sigma_m] = [\Sigma_2] \parallel [\Sigma'_1]$

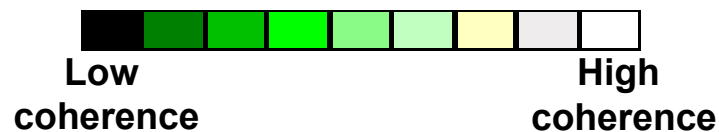
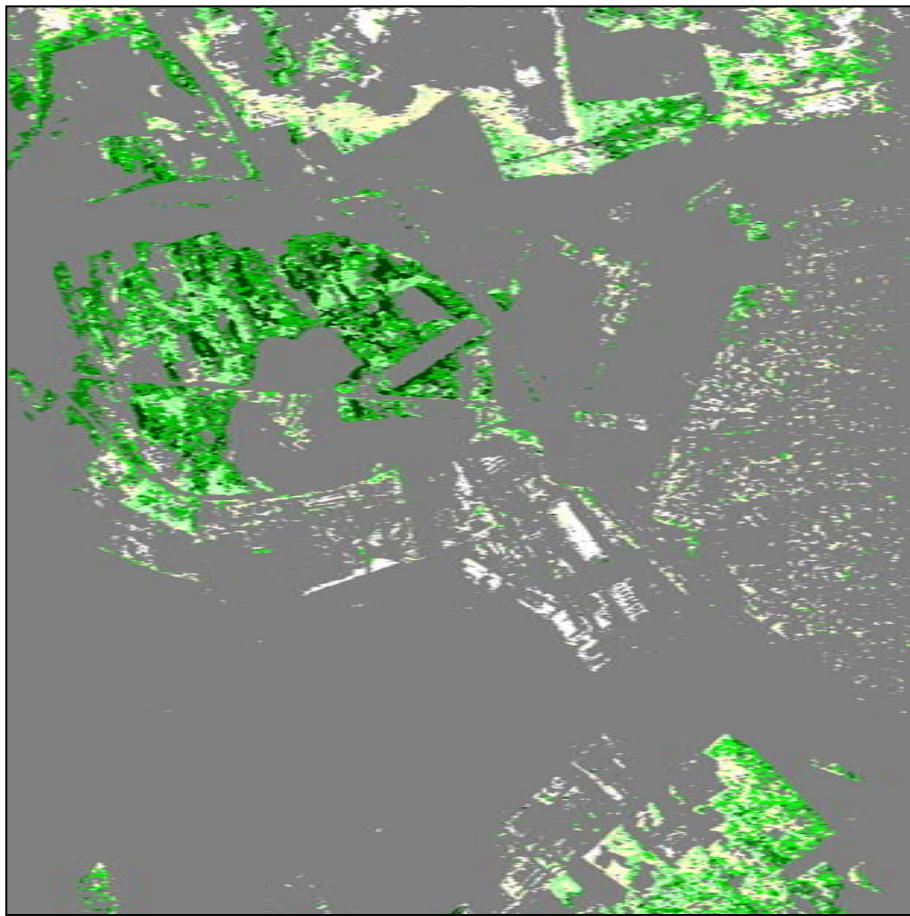
$$\begin{aligned} \text{tr}([\Sigma_m]^{-1} \langle [T_6] \rangle) = & \text{tr}([\Sigma'_1]^{-1} \langle [T'_1] \rangle) + \text{tr}([\Sigma_2]^{-1} \langle [T_2] \rangle) \\ & + \text{tr}([\Sigma'_1]^{-1} (\langle [T_{12}] \rangle - [\Sigma_{12}] [\Sigma_2]^{-1} \langle [T_2] \rangle)) \dots \\ & \dots \times \langle [T_2] \rangle^{-1} (\langle [T_{12}] \rangle - [\Sigma_{12}] [\Sigma_2]^{-1} \langle [T_2] \rangle)^{T*} \end{aligned}$$

And: $[\Sigma'_1] = [\Sigma_1] - [\Sigma_{12}] [\Sigma_2]^{-1} [\Sigma_{12}]^{T*}$
 $\langle [T'_1] \rangle = \langle [T_1] \rangle - \langle [T_{12}] \rangle \langle [T_2] \rangle^{-1} \langle [T_{12}] \rangle^{T*}$

VOLUME Scattering Mechanism Type



POL-IN-SAR Classification Results



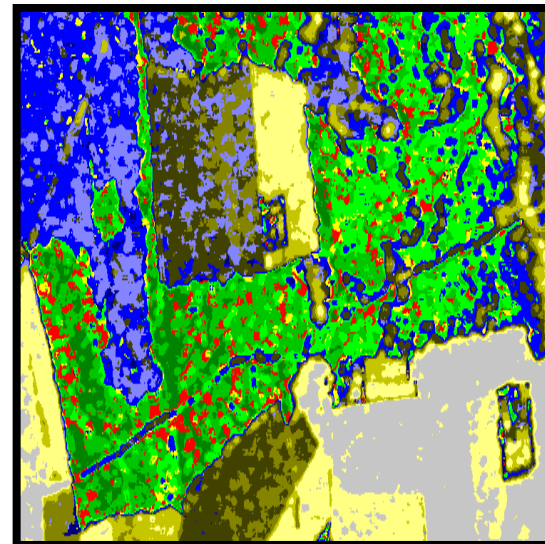
Optical Image



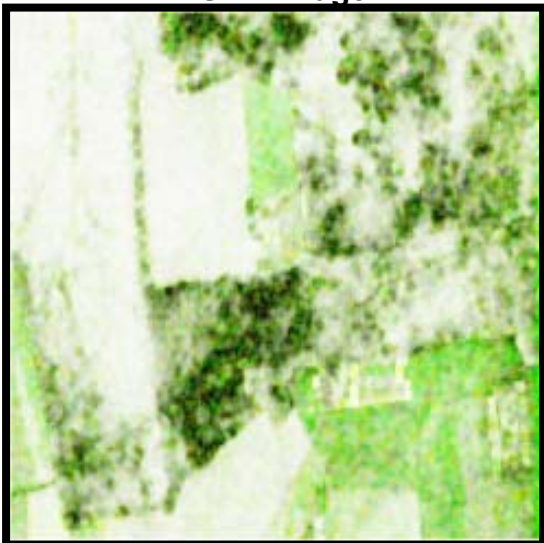
POLSAR Image



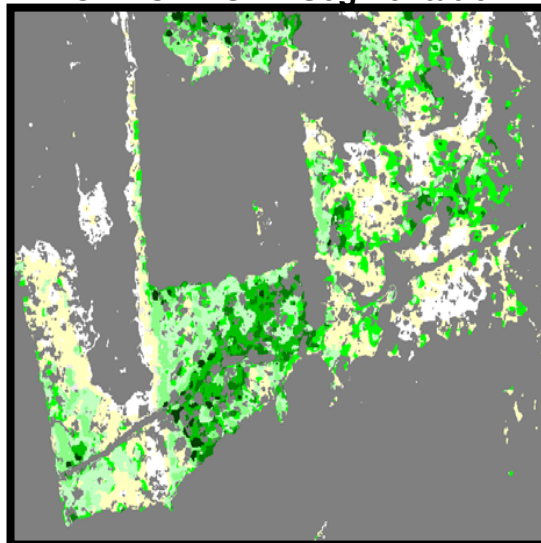
POLSAR Segmentation



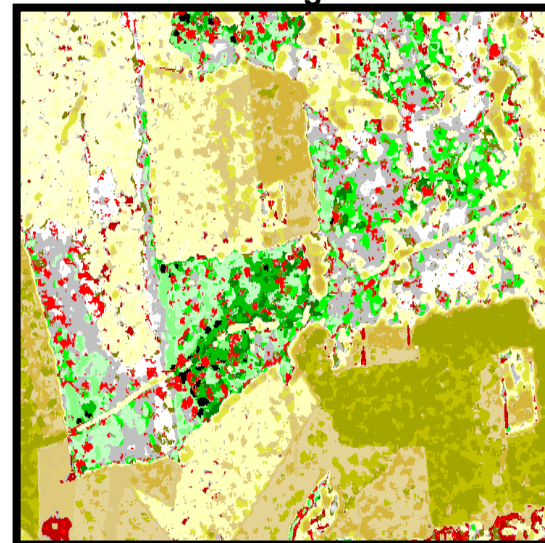
INSAR Image



VOL POLINSAR Segmentation



POLINSAR Segmentation

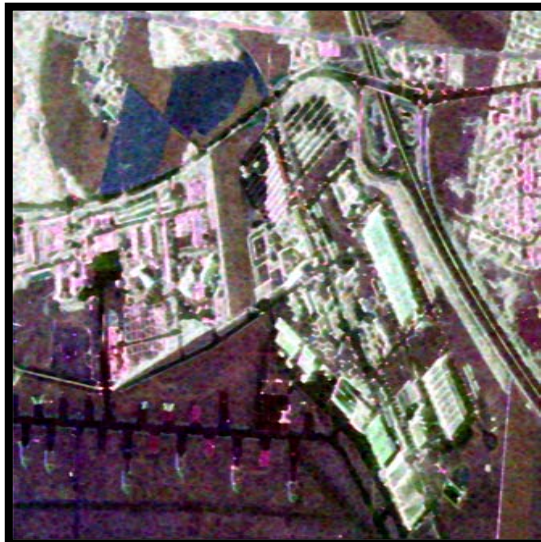


Low density forested areas segmented from dense forest

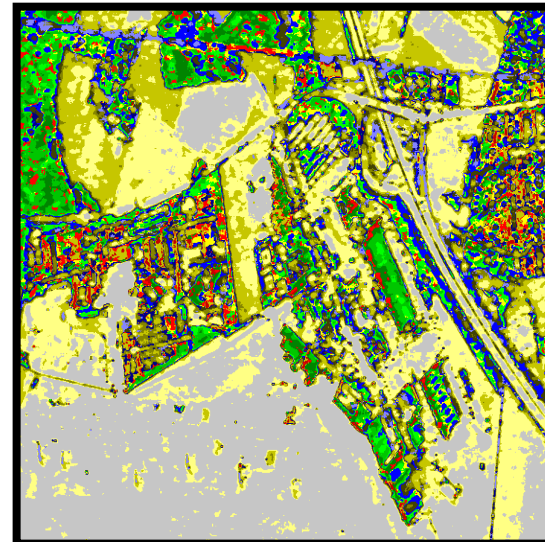
Optical Image



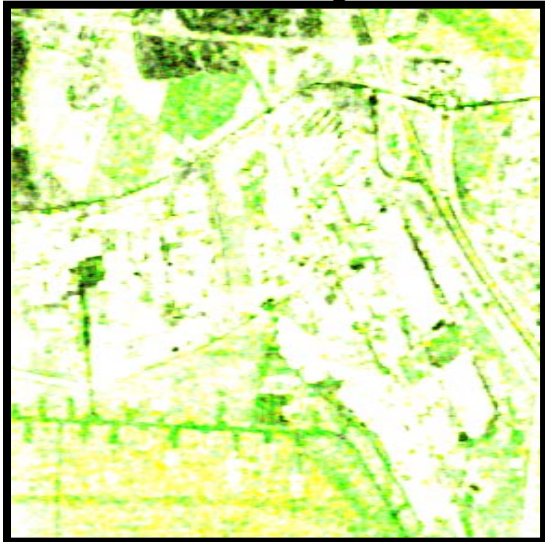
POLSAR Image



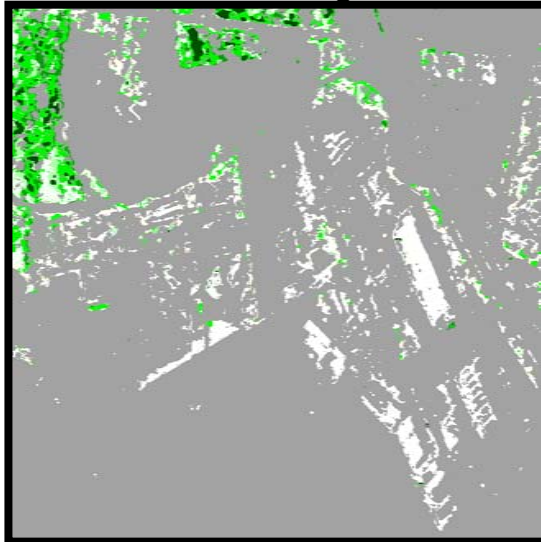
POLSAR Segmentation



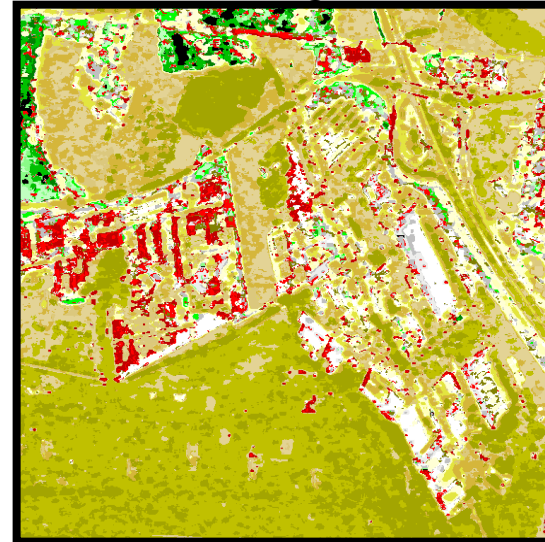
INSAR Image



VOL POLINSAR Segmentation

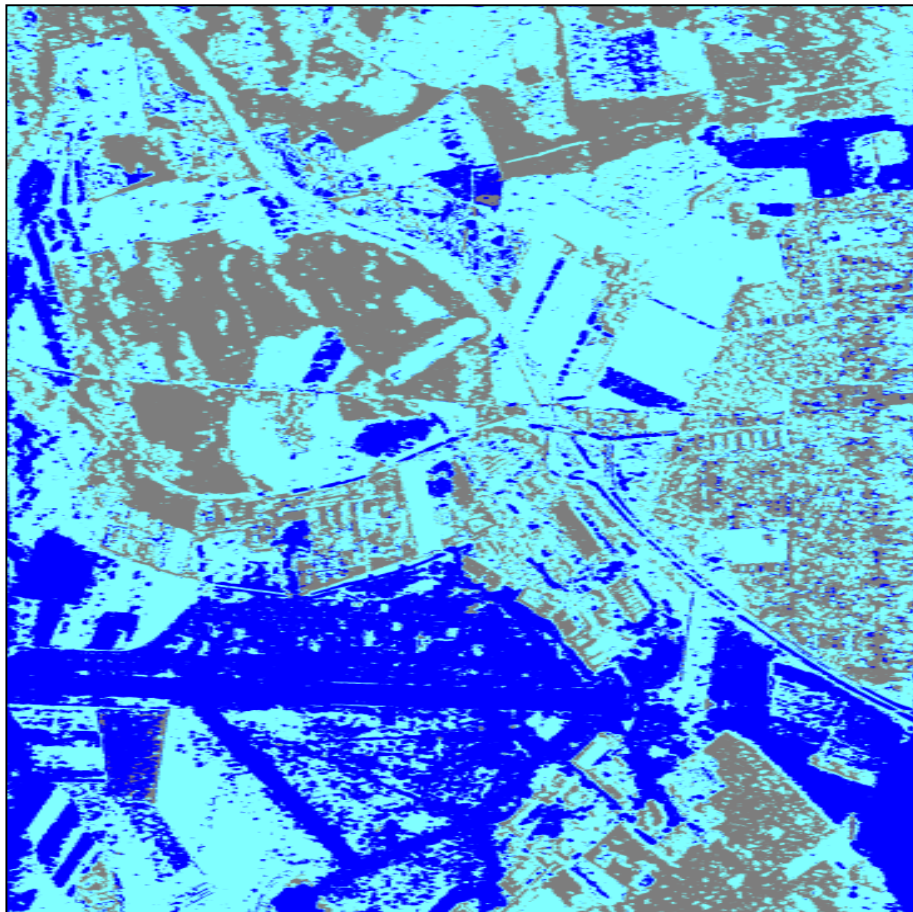


POLINSAR Segmentation

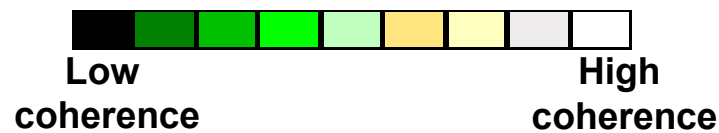


Oriented buildings segmented from vegetated areas

SURFACE Scattering Mechanism Type



POL-IN-SAR Classification Results



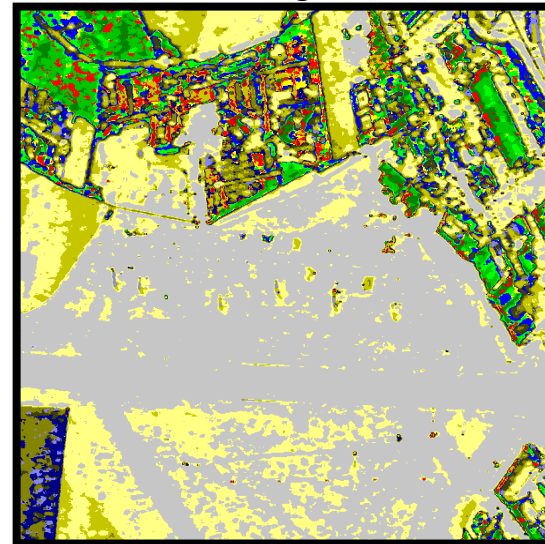
Optical Image



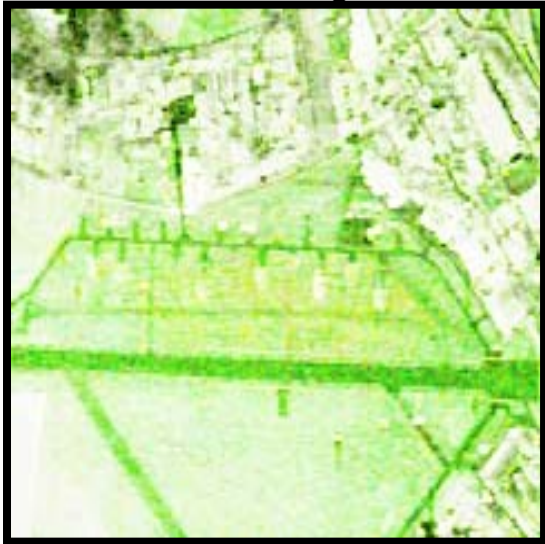
POLSAR Image



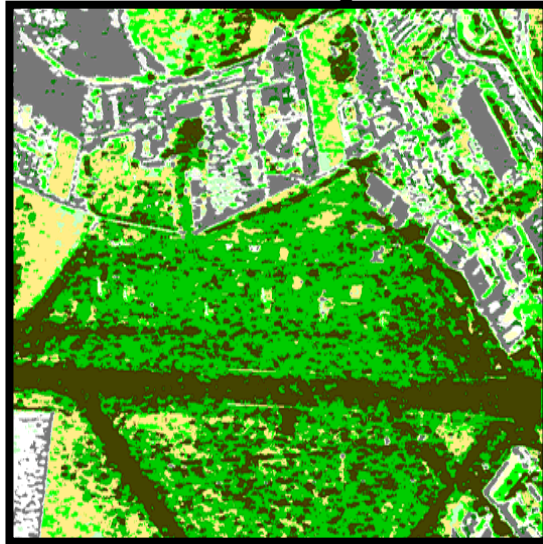
POLSAR Segmentation



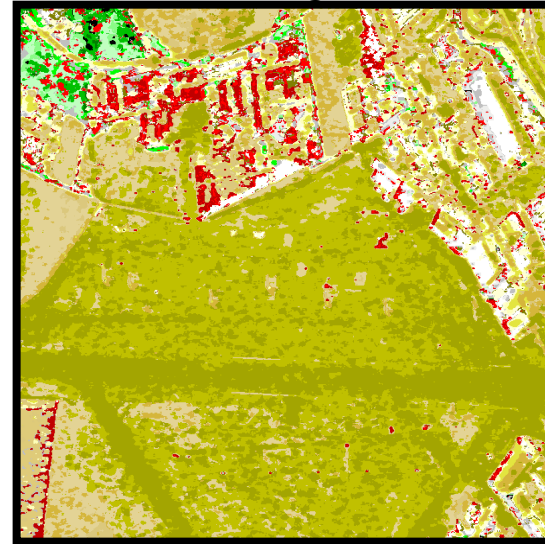
INSAR Image



DBL POLINSAR Segmentation

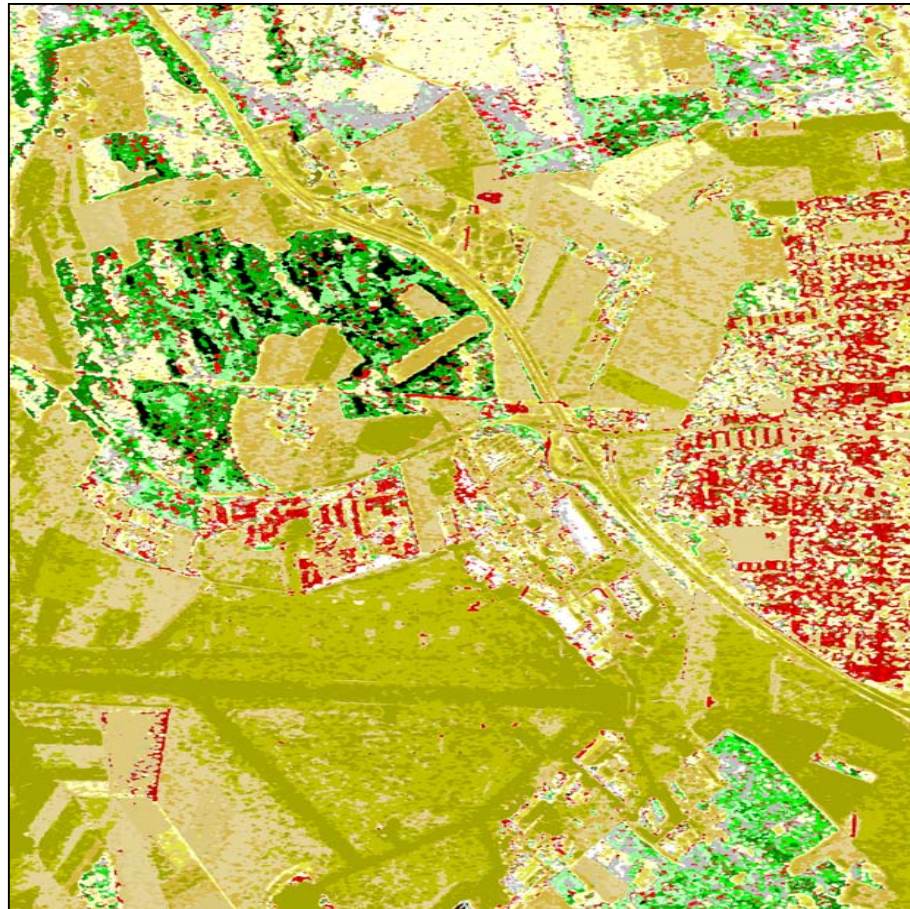


POLINSAR Segmentation



Rough surface scattering segmented from noisy areas

POL-IN-SAR Classification Results



$2A_0$

$B_0 + B$

$B_0 - B$



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POLARIMETRIC CLASSIFICATION PROCEDURE

- Unsupervised Wishart $H - A - \alpha$ segmentation procedure
- Identification of the basic scattering mechanisms

POLARIMETRIC INTERFEROMETRIC CLASSIFICATION PROCEDURE

- Segmentation of the optimum coherence spectrum
- Unsupervised 6×6 Wishart $H - A - \alpha$ segmentation procedure

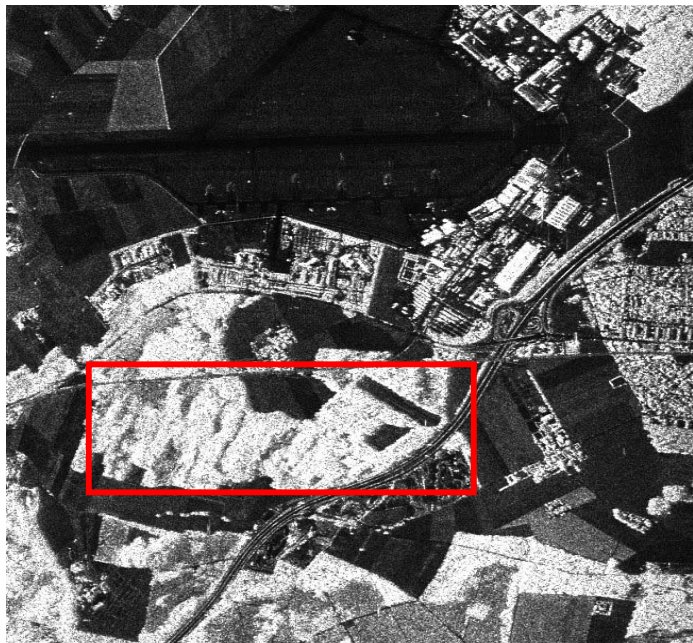
MERGING OF INTERFEROMETRIC AND POLARIMETRIC INFORMATION



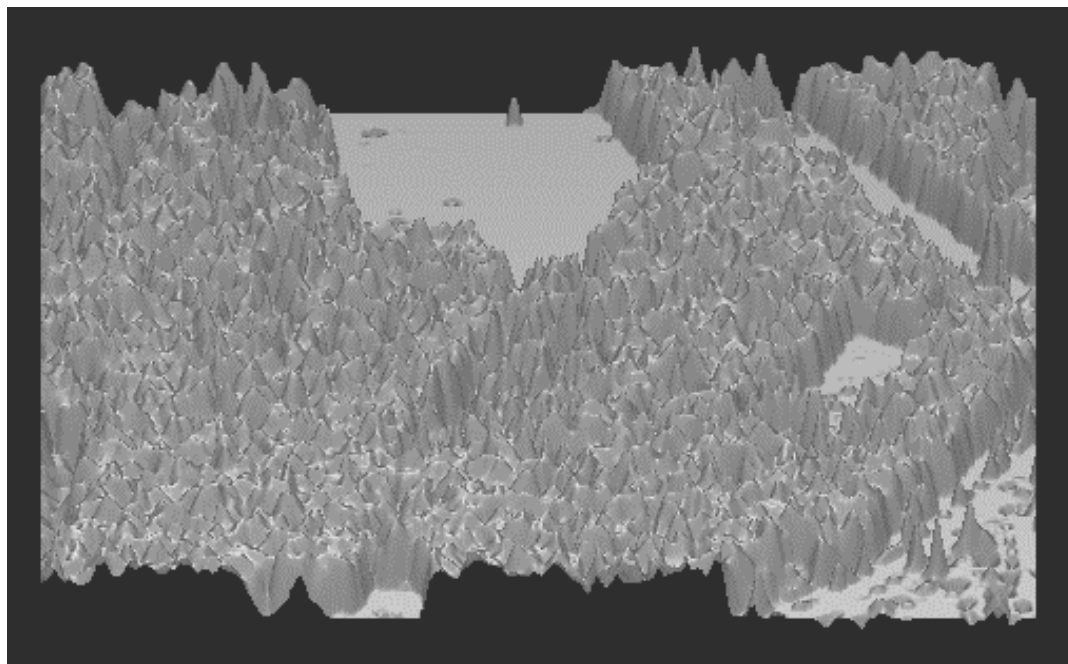
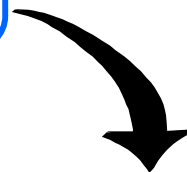
COMPLEMENTARITY AND MUTUAL CORRECTIONS



E-SAR / Test Site: Oberpfafenhoffen



INTERFEROMETRIC
POLARIMETRIC
INVERSION



3-Dimensional Forest Height Representation

Courtesy of Dr S.R. CLOUDE and Dr K. PAPATHANASSIOU

E. Pottier, L. Ferro-Famil (01/2004)

